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# Investigation of Model Predictive Control (MPC) for Steam Generator Level Control in Nuclear Power Plants

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Supervisor: Jiang, Jin, The University of Western Ontario A thesis submitted in partial fulfillment of the requirements for the Master of Engineering Science degree in Electrical and Computer Engineering © Ahmad Taemiriosgouee 2016

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## <span id="page-1-0"></span>**Abstract**

The capabilities and potential of Model Predictive Control (MPC) strategies for steam generator level (SGL) controls in nuclear power plants (NPPs) have been investigated. The performance has been evaluated for the full operating power range (0% to 100%). The specific operating conditions include: normal operations, start-ups, low power operations, load-up and load rejections. These evaluations have been carried out using a linearized steam generator dynamic model. The MPC controllers used are based on existing methodologies. Furthermore, any potential performance improvement through fine-tuning of some of the control parameters based on the dynamic characteristics of the SGL has also been investigated.

In this regard, two versions of MPC strategies have been designed and simulated. The Standard MPC (SMPC) is applied to the SGL problem first to establish the performance baseline. An Improved MPC (IMPC), by selecting appropriate values in the weight matrix of the objective function, has also been examined.

Both MPC strategies have been implemented in a Matlab Simulink environment. Their performance has been evaluated against an optimized PI controller in terms of i) set point tracking, ii) load-following in step and ramp commands, iii) figures of merits of transient responses, iv) effectiveness in rejecting disturbance from the steam and feed-water flow, and v) sensitivities to the noise in the feed-water flow measurements. The performance evaluation has been done through extensive computer simulation, and also through a set of real-time experiments on a physical mock-up steam generator level process. The results have demonstrated potential of the MPC based strategies; in particular, the IMPC strategy; for improving the performance of the steam generator level control loop.

KEYWORDS: Level Control, Non-minimum-phase, Nonlinear Model Predictive Control, Steam Generator.

## <span id="page-2-0"></span>**Acknowledgments**

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This thesis is dedicated to my lovely daughter Nastaran

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## **Symbols**









## <span id="page-14-0"></span>1 **Introduction**

Steam Generators (SGs) in a Nuclear Power Plant (NPP) play an important role in transferring heat from a fission process to steam in order to drive a steam turbine for generating power. The SG in a NPP provides an important heat sink for the reactor and for the Heat Transport System (HTS) which operates with the reactor coolant on the primary side, and the feed-water in the secondary side. It can also be used as heat removal systems in the event of an accident. From a safety point of view, the SG is a major element which isolates the primary loop (containing radioactive coolant) from the secondary loop (containing non-radioactive water and steam) to prevent water in the two systems from intermixing. The SG also prevents radioactive substances from leaking into the atmosphere in a NPP.

Other roles of a steam generator in a nuclear power plant can be summarized as follows [1]:

- Continuous cooling of the reactor core
- Mass balancing between feed-water and steam flow rate
- Preventing the carryover of impurities inside the turbine
- Generating steam for the turbine to produce electricity

A schematic diagram of a typical SG is shown in Fig.1 [2]. The hot pressurized coolant enters the inlet and passes through what is referred to as the "hot leg" of the tube bundle. The feed-water enters the secondary side of the tube bundle at the upper right of the SG through the feed-water inlet nozzle. The coolant passes through an inverted U-tube heat exchanger, where thermal energy is transferred from the primary side to the secondary side at the saturation temperature (e.g,  $250^{\circ}$ ) C at 4 MPa pressure in certain NPPs) to generate steam. The primary coolant loses thermal energy all along the U-tube. The steam passes through separators, which ensure that the exiting steam is completely dry to protect the turbine blades from damage. The water inventory in the SG can be directly measured via SG water level gauges at the secondary side.



<span id="page-15-2"></span>**Fig. 1 Schematic diagram of a typical SG in a NPP [2]**

## <span id="page-15-0"></span>1.1 **Steam Generator Level (SGL) control**

#### <span id="page-15-1"></span>1.1.1 **Importance**

The Steam Generator Level (SGL) must be controlled within a certain range and a desired value during both transient and steady-state operations to create a safe and reliable environment in a NPP. Poor control of the SGL may lead to serious consequences. If the level in the SG is too high, it may lead to the following problems: [1], [3]

- Increased moisture in the steam and carryover, and humidity to the turbine side. This increases the risk of damages to the turbine blades
- Increased potential for water hammer and water induction hazards in the piping system
- Reduced margin between the SGL and the SGL upper limit, which increases the risk of a turbine trip

If the level is too low, it may lead to the following problems: [1], [3]

- Decreased heat sink capability of the SG, which may lead to increased HTS pressure and temperature
- Jeopardized reactor cooling system due to the exposed tubes
- Reduced heat transfer capability of removing heat from the reactor, leading to reactor overheating
- SG drying-out, raising the risk of damages in SG tubes

If the control system for the SG water level is inappropriately tuned, oscillations in the water level may occur. Such oscillations can induce subsequent oscillations in:

- instantaneous turbine output power,
- feed-water and steam flow rates, and
- HTS pressure and temperature.

It has been documented [1,3,4,5] that nearly 25% of emergency reactor and turbine trips at existing NPPs are caused by poor performance in SGL control. Nearly 90% of incidents associated with SGL occur either at low operating power levels (less than 25% of full power), or during transient periods. This is mainly because of the dynamic characteristics of the SGL and the relatively higher degree of steam and feed-water flow measurement inaccuracy.

#### <span id="page-16-0"></span>1.1.2 **Unique dynamic characteristics**

The dynamics of a SGL vary considerably with changes in reactor power levels. A unique phenomenon exists particularly at low power operations, because of the dominant reverse thermal dynamic effects known as *shrink* and *swell*. A sudden increase in load will draw more steam from the SG. Naturally, one expects that the water level will decrease. However, as more steam is drawn, the bubbles in the water actually expand, and make the water level higher, which is counter-intuitive, and it makes the control system more difficult to design. This phenomenon is known as `swell`. A sudden decrease in load produces exactly the opposite response in the water level, which is called `shrink`. In the control system community, this behavior can be characterized by *non-minimal phase* dynamics in the transfer functions.

To leave sufficient operating range, it is not desirable to operate the SG at a high water level during low power operations since the SG could be subjected to an unexpectedly large step increase in the steam demand causing a large swell effect. By maintaining the SGL relatively low under a low power condition, one may accommodate a relatively large swell effect in the level without causing any risk of possible turbine trip due to inventory carryover to the turbine. Similarly, it is not desirable to operate the SG at a low water level during high power operations since the SG may be subjected to an unexpectedly large step decrease in the steam demand, causing a large shrink to uncover the HTS U-tubes in the heat exchanger. Consequently, by maintaining the SG water level relatively high at high power, one can accommodate a relatively large shrink in level without increasing the risk of exposing the U-tube heat exchanger. Hence, the above guidelines should be followed in selecting swell based set points, i.e., the desirable set point values for the steam generator levels.

The swell and shrink effects decrease as the operating power level increases. This is one of the main reasons that the conventional Steam Generator Level Control (SGLC) schemes (single-element/three-element control) cannot possibly cover the entire operating power range (from 0% to 100%). Other characteristics of the SGL that may affect controller design include [1]:

• highly nonlinear behavior, especially during low power operations,

- tight constraints on the SG input (feed-water flow rate) and the SG output (SGL), and
- inaccurate and noisy measurements for feed-water flow rate and steam flow rate during low power operations.

It may be noted that due to the lack of an effective control system that can cover the entire operating power range, manual control is often applied to the SGL system during the start-up and the low power operations in many existing NPPs.

## <span id="page-18-0"></span>1.2 **Motivations for the current work**

The SGL control system designs have been extensively investigated and substantial efforts have been made to prevent costly reactor shutdowns caused by the SGL control system. Over the last thirty years, a great deal of research has been done with the SGLC, and many advanced model-based SGL controller design have been proposed in the literature that include

- Model predictive control (MPC)
- Model reference adaptive PID
- Linear quadratic regulator method
- Fuzzy and neuro-fuzzy control
- Artificial neural network based controller
- $\bullet$  H<sub>∞</sub> control techniques
- Gain-scheduling controller
- Extension of MPC principle
- Auto-tuned PID
- Auto adaptive predictive controller

Model based control strategies for the SGL control presented in the existing literature often investigate the performance of the given scheme on a limited number of SGL control scenarios. Much of the literature does not evaluate the performance of the control scheme during the start-up and the low power

operations. Extensive evaluation for the SGLC performance under tight constraints, and under steam and feed-water flow disturbances are often not done. Furthermore, the capability of the SGL control for load following in steps and in ramps, as well as for load rejections are also not properly investigated and evaluated in most of the existing literature. It is noted that, despite many advanced control techniques developed for SGL, they have rarely been used in NPPs, as their ability to handle the entire range of operating modes (including start-up, low power operations, and emergency shut-downs) has not yet been extensively evaluated and demonstrated.

For a proper evaluation, a control scheme must be investigated with respect to all operating and transient conditions of a SG. Therefore, it is reasonable to perform an in-depth study in order to understand the capability of a given control scheme to deal with the challenges in the SGL control in NPPs. One model based advanced control strategy that has been used in many other industrial control applications is the *Model Predictive Control (MPC)*. The MPC based approaches make use of the "best knowledge" of the process dynamic in order to deliver an effective performance by the control system. Due to the capabilities of the MPC based approaches to handle challenging control problems, the MPC has been selected for an in-depth evaluation, while applying it in the SGL control systems in NPPs. Furthermore, in addition to the detailed performance evaluation of existing advanced MPC controllers, it would be interesting to investigate if a MPC controller performance can be improved by applying customized fine-tuning of the control parameters by taking into account the specific characteristics of the SGL in NPPs at different power levels.

#### <span id="page-19-0"></span>1.3 **Objectives, approaches, and scope**

The objective of this study is to perform a detailed evaluation of the MPC based strategies for the SGL control in NPPs. Performance has been evaluated for a MPC controller based on existing advanced methodologies. Furthermore, any performance improvements that can be achieved by the fine-tuning of the control parameters (based on the characteristics of the SGL) of the existing MPC approaches has also been investigated. The investigation have been performed to cover all operating conditions of a SG in a NPP that include normal operations, as well as start-ups, low power operations, load-up and load rejections.

The control performance of the MPC based methodologies have been evaluated through computer simulation and through a set of tests on a physical mock-up steam generator level process that uses a metal plate and pressurized air to simulate the effect of a SGL in a NPP. This mock-up steam generator has been referred to as the Plate Level System (PLS) in this thesis. The PLS closely simulates the characteristics of an actual SGL (based on Irving model) at different power levels.

The scope of this work has been limited to an in-depth performance evaluation of existing advanced MPC based methodologies for SGLC in NPPs. It is well known that the MPC based approaches rely heavily on the model of the underlying process. Although there are a few models for the SGL exists in the literature; however, this study has limited its scope to the Irving model for the SGL. Therefore, the results reported in this study are all based on the Irving model. Furthermore, the Irving model specifies the SGL model parameters only at five different power levels (5%, 15%, 30%, 50%, and 100%). The MPC based strategies implemented for evaluation in this study are centered around these power levels only.

#### <span id="page-20-0"></span>1.4 **Thesis contributions**

To investigate the performance of the MPC based approaches, two versions of the MPC controllers have been designed and implemented in Matlab Simulink environments. The first implementation has been done by using existing advanced MPC methodologies. This implementation has been referred to as 'Standard MPC (SMPC)" in this thesis. The second implementation make use of proper feedbacks from states to further improve the control performance by i) first optimizing a cost function, and ii) then by selecting proper values for the manipulated control signal

 $u(k)$ . This control signal is then applied to the Feed-water Control Valve (FWCV). The second MPC has been referred to as "Improved MPC (IMPC)".

Both computer simulation, and the Plate Level System (PLS) physical tests have been performed to include all operating conditions of a real NPP. The performance has been evaluated in terms of several performance measures that include set point tracking, overshoot, undershoot, settling time subject to set point change, transient response and load following.

During the process of implementation, the following contributions are made:

- Linearization of the SGL model and design of power level dependent parameters for SMPC/IMPC schemes
- Selection of an appropriate cost function  $J$  that can be used to minimize the prediction of the error signal over the future horizon of  $p$ , and also minimizes the usage of the controller outputs in the least-square sense
- Application of "Laguerre functions" as an efficient tool for approximating stable dynamic systems for the SMPC and the IMPC controller structures.
- Presented a simple approach to define the weight matrix  $Q_{IMPC}$  for IMPC.

#### <span id="page-21-0"></span>1.5 **Organization of the thesis**

The organization of the thesis is as follows: Chapter 1 introduces the importance of the SGL control in nuclear power plants, and has outlined the work done in this thesis. In Chapter 2, an overview of the steam generator level control, and a brief literature review are presented. In Chapter 3, the details of SMPC and IMPC methodologies, along with the mathematical model of the SGL are discussed. Model linearization is also presented in Chapter 3. Performance of the SMPC and the IMPC methodologies have been investigated through computer simulation in Chapter 4. The results of the experiment on the PLS are presented in Chapter 5. And finally, conclusions are drawn in Chapter 6 with a brief discussion.

## <span id="page-22-0"></span>2 **Literature Review**

## <span id="page-22-1"></span>2.1 **Steam generator level control**

To maintain a constant water mass inventory in the SG at different power levels, and to reduce the SGL fluctuations (due to, e.g., swell or shrink in transient modes load following, reactor set-back, and step-back), the SGL set-point needs to be calculated in a dynamic manner and adjusted according to the operational power level. A dynamic SGL set-point allows the SGL control system to react in the same direction as the power change. In a fixed SGL set-point, the SGL would rise when the power is increased suddenly (due to the swell effect). In a fixed set-point system, this level rise would be opposed by the feed-water supply decrease in an attempt to lower the SGL back to the fixed set-point. Now, when the temporary swell effect subsides, the collapse of the steam bubbles and the decrease in the inventory supply would have to be reversed in order to supply more feed-water at the increased load in an attempt to maintain the desired inventory. If the set-point of the SGL is made dynamic, the above scenario can be effectively reduced. The original steam demand increase will cause a swell effect but, at the same time, the increase in power level would be recognized to request a high SGL set-point. As a result, the swell effect (level increase) can be matched by the level set-point increase so that little-to-no change in the control signal would be initiated at the onset of such disturbances. More specifically, the difficulties in designing an effective level control system for a SG can be summarized as follows:

#### *Nonlinear plant characteristics*

The dynamic behaviors of a SG are highly nonlinear. A set of linearized dynamic models can be obtained at different reactor power levels. However, the parameters in these linearized models vary significantly as the reactor power changes. The nonlinear process dynamics complicate the design of an effective SGL control system. A possible solution is to design a set of controllers for different power levels and then to apply "gain-scheduling" techniques in order to select an appropriate controller based on the operating power level.

#### *Non-minimum-phase plant characteristics*

A SG exhibits inverse response behavior, which is represented by a non-minimum phase dynamic process. This is particularly predominant at the low operating power range. This non-minimum phase characteristic limits the achievable system performance, and can significantly complicate the design process of an effective SGL control system.

#### *Flow measurement errors*

It is well known that at low power operations (0-25% of the full power, FP), the measurements of the main steam-flow and the feed-water flow are noisy and unreliable. The SGL is more sensitive to disturbances at low power levels. As a result, the SGL control at low power levels is even more challenging.

#### *Tight performance constraints*

The water level in a SG has to be maintained within specific limits in order to avoid turbine and reactor trips. Moreover, transients or oscillations in the level must be minimized to prevent turbine and reactor power oscillation. This problem is compounded by a lack of accurate information on the feed-water flow rate and the steam flow rate for the control system to use. In practice, there are explicit limits due to physical constraints on the magnitude of change in the feed-water flow rate.

It is noted that conventional three-element controllers may not be able to handle the SGL effectively at low power level operations. This is because, in addition to the nonlinearity and non-minimum phases, at low power, both steam and feed-water flow rate signals become noisy and un-reliable. This prevents the three-element controller from stabilizing the system. The controller, with only proportional and integral water level measurement terms, lacks the predictive capability to anticipate the reverse dynamics of the water level, and therefore results in instabilities.

### <span id="page-24-0"></span>2.2 **SGL control strategies in the literature**

The SGL control designs literature has spread over the last thirty years. Many advanced design approaches have been proposed in the literature in order to solve the SGL control problems. For example, the design of a suboptimal controller using linear output feedback control [5]. A PID control strategy is proposed in [7] which uses an observer to estimate the water inventory. A more general gain-scheduled linear quadratic Gaussian with loop transfer recovery (LQG/LTR) controller is proposed in [3]. A SGL control system based on fuzzy logic principles has also been investigated. In fact, a fuzzy logic based SGL controller has been installed at the Fugen NPP [8]. A neuro-fuzzy controller is proposed in [9], which uses a multilayer artificial neural network with special types of fuzzifier, inference engine, and defuzzifier. A robust fuzzy logic gain-scheduler is designed in [10] based on the synthesis of fuzzy inference and  $H_{\infty}$  control techniques. A fuzzy logic controller which is tuned off-line with genetic algorithms using SGL, feed-water and steam flow rate signals is proposed in [11].

A gain-scheduling controller has been proposed in [12]. A novel architecture for integrating artificial neural networks with industrial controllers is proposed for use in predictive control of a SG [13]. In this method, a PID controller is used to control the process and a recurrent neural network is used to model the process as a multistep-ahead predictor. An adaptive predictive controller is proposed in [14], where a recursive least-squares parameter estimation algorithm is used to estimate the unknown parameters of the SG model. The obtained model is then used to design a generalized predictive controller.

MPC based controls for the SGL has also been presented in the literature. Irving *et al.* developed a linearized model with power-dependent parameters in order to describe the U-tube SG dynamics over the entire operating power range. Many model based controllers proposed in the literature has used the Irving model as the SGL model in order to evaluate the performance of the proposed controller. A controller based on an extension of the MPC principle is developed in [15]. An auto-tuned PID controller using a MPC method is also investigated in [16].

In the following, details of the literature survey that establishes concepts and techniques related to advanced control system design for SGL are discussed.

#### <span id="page-25-0"></span>2.2.1 **Auto-tuned PID controller using a MPC**

In an auto-tuned PID controller, PID control gains are automatically tuned to overcome the drawbacks of the conventional PID controller with fixed control gains. This is done by changing the input-weighting factor according to the power level using a MPC method. This approach has been investigated for the SGL by Man Gyun Na [17]. An MPC-based PID controller has been derived from the second order linear model of a process. The SG has been described by the wellknown 4<sup>th</sup> order linear model which consists of the mass capacity, reverse dynamics and mechanical oscillations terms. But the important terms in this linear model are the mass capacity and reverse dynamics terms, both of which can be described by  $a$  2<sup>nd</sup> order linear system. The proposed controller was applied to a linear model of the SG. The parameters of a linear model for the SG can be changed according to the operation power level.

#### <span id="page-25-1"></span>2.2.2 **Linear Quadratic Regulator (LQR)**

The Linear Quadratic Regulator (LQR) controller is developed using local linearization of the SG model and then scheduling gain to cover the entire range [16]. [Le Wei](http://ieeexplore.ieee.org/search/searchresult.jsp?searchWithin=%22Authors%22:.QT.Le%20Wei.QT.) and [Fang Fang](http://ieeexplore.ieee.org/search/searchresult.jsp?searchWithin=%22Authors%22:.QT.Fang%20Fang.QT.) have proposed a  $H_{\infty}$ -based LQR control for the SGL [18]. A continuous time model of the SGL is used, and LQR and H∞-based control scheme technique is applied to design an optimum controller that forces the SGL to follow a desired set point. The Irving Model is used for the SGL. It has been shown in [6] that the proposed approach can provide set point tracking ability of the SGL at different loads.

#### <span id="page-26-0"></span>2.2.3 **Fuzzy and Neuro-Fuzzy based controllers**

An adaptive neuro-fuzzy logic controller (NFLC) can also be used for SGL control. B.H. Cho and H.C. No have proposed a design of stability–investigated neuro-fuzzy logic controllers for nuclear steam generators [9]. A neuro-fuzzy algorithm, which is implemented by using a multilayer neural network with special types of fuzzifier, inference engine and defuzzifier, is applied to the SGL. This type of controllers has the structural advantage that arbitrary two-input, single-output linear controllers can be adequately mapped into a set of specific control rules. In order to design a stability-investigated NFLC, the stable sector of the given linear gain is obtained from Lyapunov's stability criteria. Then this sector is mapped into two linear rule tables that are used as the limits of NFLC control rules. The automatic generation of NFLC rule tables is accomplished by using the back-error-propagation (BEP) algorithm. There are two separate paths for the error back propagation in the SGL. One path considers the level dynamics depending on the SG capacity, and the other takes into account the reverse dynamics of the SG. The amounts of error back propagated through these paths show opposite effects in the BEP algorithm from each other for the swell-shrink phenomenon.

#### <span id="page-26-1"></span>2.2.4 **Gain scheduled controller**

In a gain scheduled controller, the controller parameters may vary according to system operations. The control law is in the form of a parameter-dependent nonlinear state-feedback control. Kim *et al.* have proposed a gain–scheduled L<sub>2</sub> control strategy for nuclear steam generator SGL [12], and have designed a nonlinear gain-scheduled controller for the SGL which covers the entire operating envelope. Numerically linearized models of the SGL have been developed using a validated nonlinear model that covers its entire operating envelope. The linear quadratic Gaussian with loop transfer recovery (LQG/LTR) method is used to design dynamic compensators for each of the linearized models. The various compensator matrices are fitted to a scheduling variable, namely, the temperature difference between the primary side hot- and cold-leg temperatures, resulting in a gain-scheduled nonlinear compensator. The performance of the gain-scheduled

compensator (GSC) is systematically investigated via transient response simulation using the nonlinear SGL model.

#### <span id="page-27-0"></span>2.2.5 **H∞ control techniques**

J. J. Sohn and P. H. Seong have presented a robust *H<sup>∞</sup>* controller for the feed-water system of the Korean Standard Nuclear Power Plant (KSNP) [19]. A series of experiments has been performed using the developed thermal–hydraulic model in order to acquire the input–output data sets, which represent steam generator characteristics. These data sets are utilized to build simplified steam generator models for control via a system identification algorithm. The representative robust controllers for the selected models are designed utilizing the loopshaping  $H_{\infty}$  design technique and, the robustness and performance of the proposed controllers are validated and compared against those of PI (proportional–integral) controller.

#### <span id="page-27-1"></span>2.2.6 **Extension of the MPC principle**

MPC is a control strategy in which the current control action is obtained at each sampling time and a finite horizon open-loop optimal control problem, by using the current state of the plant as the initial state. The optimization algorithm uses the predicted process outputs in order to find the sequence of process inputs values (over a future interval known as the "control move horizon") that solves a predefined constrained optimization problem. Then the optimization yields an optimal control sequence. Kothare *et al.* have proposed "Level control in the steam generator of a nuclear power plant," [6], and have presented a framework for addressing this problem based on an extension of the standard linear model predictive control algorithm to linear parameter varying systems.

## <span id="page-27-2"></span>2.3 **Summary**

The characteristics of the SGL, and the factors that may affect the performance of a SGL control system have been reviewed in this chapter. A number of advanced methodologies for the SGL control proposed in the literature has also been reviewed.

## <span id="page-28-0"></span>3 **MPC for SGL Control**

#### <span id="page-28-1"></span>3.1 **Overview**

The Model predictive control (MPC) has been widely investigated and used in the process industry as an advanced control methodology. The MPC methodology has received significant attention for optimizing the performance of control systems, such as the SGL control due to several advantages that include

- the ability of the MPC design to yield high performance control systems capable of operating without operator interventions, and
- the ability to allow constraints to be imposed on inputs, states and outputs.

The MPC uses predictions of future behavior of the process to make anticipated control decisions. This prediction capability allows for optimally solving a control problem on line, where the difference between the predicted output and the desired reference is minimized over a future horizon. The control problem can be subjected to constraints, on the manipulated inputs and outputs. The MPC utilizes a process model to make a prediction of future plant behavior, and to compute the appropriate corrective control action required to drive the predicted output as close as possible to the desired target value (set-point). The objective is to find the future trend for the input (control actions) that moves the future trend of the output so that it approaches the desired reference trajectory.

In a MPC scheme, the current control action is obtained by solving a finite horizon open-loop optimal control problem at each sampling instant, by using the current state of the plant as the initial state. The optimization algorithm uses the predicted process outputs in order to find the sequence of process input values (over a future interval known as control move horizon) that solves a predefined constrained optimization problem. Then the optimization yields an optimal control sequence and the first control in this sequence is applied to the plant. Such a principle, characterizing the basic philosophy of MPC for SGL is illustrated in Fig. 2 [20].



**Fig. 2 Basic feed-back structure of MPC**

<span id="page-29-1"></span>The MPC based methodologies require a model of the process. More accurate models lead to more enhanced control performance of the MPC. In the following, the SG model used in this work is discussed.

## <span id="page-29-0"></span>3.2 **Mathematical model of a steam generator**

The design of an effective controller depends on the availability of accurate mathematical models describing the plant dynamics. The model should be accurate enough, and be sufficiently simple but still be able to capture the essential SG dynamics. In this research, the Irving model [1], [3] is used because it has met the above criteria and has widely been used in the design and evaluation of SG control systems. The Irving model captures the non-minimum phase behavior of the SG level.

The Irving model is a linear fourth-order dynamic model whose parameters depend on the reactor/turbine power level. The transfer function relating the feed-water flow rate,  $q_w(s)$  and the steam flow rate,  $q_v(s)$  to the SG water level,  $Y(s)$  can be expressed as [1]:

$$
Y(s) = \frac{G_1}{s} (Q_w(s) - Q_v(s)) - \frac{G_2}{(1 + \tau_2 s)} (Q_w(s) - Q_v(s))
$$
  

$$
\frac{G_3 \times s}{\tau_1^{-2} + 4\pi^2 T^{-2} + 2\tau_1^{-1} s + s^2} \times Q_w(s)
$$
 (1)

where  $Y(s)$  represents the SG level,  $\tau_1, \tau_2$  and T are the damping time constants and the period of the mechanical oscillation, respectively. The first term in Eqn. (1) represents the effect of any mass imbalance (feed-water vs steam flow) in the SG level. It takes into account the level change due to the mass difference from the feed-water inlet to the steam outlet.  $G_1$  is a positive constant independent of the power level.  $G_2$  is the magnitude of the swell or shrink due to the feed-water or steam flow rates, and is a positive parameter which is also dependent on the power level.  $G_3$  is the magnitude of the mechanical oscillation, and is a function of the power level. The parameter  $G_3$  is positive and is also a function of the power level.

Irving model specified the parameters at five different power levels, 5%, 15%, 30%, 50% and 100%. These parameters are listed in Table 1. [1].

$\theta$	5%	15%	30%	50%	100%
$G_{1}$	0.058	0.058	0.058	0.058	0.058
$G_2$	9.63	4.46	1.83	1.05	0.47
$G_3$	0.181	0.226	0.310	0.215	0.105
$\tau_1$ (sec)	41.9	26.3	43.4	34.8	28.6
$\tau_2$ (sec)	48.4	21.5	4.5	3.6	3.4
$T$ (sec)	119.6	60.5	17.7	14.2	11.7
$q_{v}$ (kg / sec)	57.4	180.8	381.8	660.0	1434.7

<span id="page-30-0"></span>**Table 1 The parameters of Irving SG model over five power levels**



<span id="page-31-1"></span>**Fig. 3 SGL to (a) step changes in the feed-water flow, (b) step changes in the steam flow based on the Irving model [1]**

The responses of the SGL to step changes in the feed-water flow rate and the steam flow rate at different power levels, based on the Irving model, are shown in Fig. 3 [1]. The inverse response behavior, and the nonlinear characteristics of the SGL are clearly observed in the figure, especially at the low power levels. For example, at 5% FP, when the feed-water flow rate is increased, the level response first undergoes undershoot, before rising up (Fig. 3(a)). Similar responses, but in the reverse direction, are seen in Fig. 3(b) when the steam flow rate is increased.

## <span id="page-31-0"></span>3.3 **SGL model linearization**

To design a control algorithm for the SGL, the SG model needs to be linearized. The dynamics of the SGL under different power levels are different, and hence, different sets of parameters have to be used.

In this investigation, five different power levels, based on the Irving model, are considered. The corresponding parameters under these power levels are determined through system estimation and model-matching techniques. The Irving model linearized in this study may be viewed as five piecewise Linear Parameter Varying (LPV) models, to cover five power regions shown in Table 2.

<span id="page-32-0"></span>

<b>Region</b> #	<b>Power level covered</b>		
<b>Region 1</b>	$0\% < \theta \le 8\%$		
<b>Region 2</b>	$8\% < \theta \le 20\%$		
<b>Region 3</b>	$20\% < \theta \leq 40\%$		
<b>Region 4</b>	$40\% < \theta \le 75\%$		
<b>Region 5</b>	$75\% < \theta \le 100\%$		

**Table 2 SGL model linearization regions**

From Eqn. (1), one can represent the system as:

$$
G_{u}(s) = \frac{G_{1}}{s} - \frac{G_{2}}{(1 + \tau_{2}s)} + \frac{G_{3} \times s}{\tau_{1}^{-2} + 4\pi^{2}T^{-2} + 2\tau_{1}^{-2}s + s^{2}},
$$
  
\n
$$
G_{v}(s) = -\frac{G_{1}}{s} + \frac{G_{2}}{(1 + \tau_{2}s)}
$$
\n(2)

where  $G_u(s)$  and  $G_v(s)$  are the transfer functions. By using the linearization method to identify the SGL model within a power region, the model is assumed to be linear and time-invariant. The state equations of the Irving's SG model are as follows:

$$
\dot{x}_1(t) = G_1(q_w(t) - q_v(t))
$$
\n
$$
\dot{x}_2(t) = \tau_2^{-1}x_2(t) - \frac{G_2}{\tau_2}(q_w(t) - q_v(t))
$$
\n
$$
\dot{x}_3(t) = 2\tau_1^{-1}x_3(t) + x_4(t) + G_3q_w(t)
$$
\n
$$
\dot{x}_4(t) = -(\tau_1^{-2} + 4\pi T^{-2})x_3(t)
$$
\n
$$
y(t) = x_1(t) + x_2(t) + x_3(t)
$$
\n(3)

Denoting the feed-water and the steam flow rates by  $u(t) = q_w(t)$  and  $d(t) = q_v(t)$ Eqn. (1) can be converted into the following state space form in continuous domain:

$$
\dot{x}(t) = A'(\theta)x(t) + B'(\theta)u(t) + B'_{d}(\theta)d(t)
$$
\n
$$
y(t) = C'x(t)
$$
\n
$$
A'(\theta) = \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & a_{22} & 0 & 0 \\ 0 & 0 & a_{33} & a_{34} \\ 0 & 0 & 1 & 0 \end{pmatrix}, \ B'(\theta) = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \\ 0 \end{pmatrix}, \ B'_{d}(\theta) = \begin{pmatrix} -b_1 \\ -b_2 \\ 0 \\ 0 \end{pmatrix}, \ C' = \begin{pmatrix} 1 & 1 & 0 \end{pmatrix}
$$
\n(5)

where

$$
a_{34} = -\tau_1^{-2}(\theta) - 4\pi^2 T^{-2}(\theta)
$$
  
\n
$$
b_1 = G_1(\theta), b_2 = -G_2 / \tau_2(\theta), b_3 = G_3(\theta)
$$
  
\n
$$
a_{22} = -1 / \tau_2(\theta)
$$
  
\n
$$
a_{33} = -2 / \tau_1^{-1}(\theta)
$$
\n(6)

## <span id="page-33-0"></span>3.4 **The MPC for SGL control**

The MPC controller for the SGL computes the manipulated control signal at each sampling time by solving a finite horizon open-loop optimal control problem, using the states of the plant. A sequence of optimal control signals is computed. The basic feedback control structure of MPC for SGL in shown in Fig. 4.



<span id="page-33-1"></span>**Fig. 4 Basic feedback control structure of MPC for SGL**

The MPC uses the SGL model to predict the future response of the SGL. The basic philosophy of MPC is shown in Fig. 5. The SGL model is used to predict the future states and output  $x(k+i|k)$ ,  $y(k+i|k)$ ,  $i=1,...p$  of the system over the timehorizon  $p$ , as shown in Fig. 5. When the manipulated variable (feed water flow rate)  $u(k+i|k)$ ,  $i = 0,1,...m-1$  is changed over some future time-horizon, i.e., the control horizon *m*, using these predictions, *m* control signals  $u(k+i|k)$ ,  $i = 0,1,...m-1$  are computed to minimize the performance index over the prediction horizon p. The first control signal (action) in the sequence, i.e.,  $u(k|k)$ , is then applied to the Feed-water Control Valve (FWCV). The remaining optimal inputs are discarded, and a new optimal control problem is solved at each sampling time.



**Fig. 5 Basic philosophy of a MPC**

<span id="page-34-0"></span>The cost function can be defined as the quadratic error between the future reference variable and the future controlled variable within the chosen discrete time horizon *m* as follows:

$$
J_{p}(k) = \sum_{i=1}^{p} (r(k+i|k) - y(k+i|k))^{T} Q_{y}(r(k+i|k) - y(k+i|k))
$$
  
+
$$
\sum_{i=1}^{m-1} u(k+i|k)^{T} R_{u} u(k+i|k) + \sum_{i=1}^{m-1} \Delta u(k+i|k)^{T} R_{\Delta u} \Delta u(k+i|k)
$$
 (7)

where  $r(k)$  is the SGL set-point,  $y(k)$  is the SGL measurement (controlled variable), *u* is feed-water flow rate (manipulated variable) and  $Q_y$ ,  $R_u$ ,  $R_{\Delta u} \ge 0$  are the weighting matrix. The performance-index or cost-function  $J_p(k)$  in Eqn. (7) reflects the tracking error between the reference and the measured SGL. It also includes the control effort in terms of signals going to the FWCV. Subject to the following constraints on the control input,  $u(k+i|k)$ ,  $i = 0,1,...m-1$ , states and output  $x(k+i|k)$ ,  $y(k+i|k)$ ,  $i = 1,...p$ :

$$
u_{j,\min} \le u_j(k+i|k) \le u_{j,\max} \qquad j=1,2,\cdots,n_u, i=0,1,\ldots,m-1
$$
 (8)

$$
\left|\Delta u_j(k+i|k)\right| \le \Delta u_{j,\max} \qquad j=1,2,\cdots,n_u, i=0,1,\ldots,m-1 \tag{9}
$$

where  $u_{j,\text{min}}$  and  $u_{j,\text{max}}$  are minimum and maximum limits of control signal, and

$$
\Delta u(k+i|k) = u(k+i|k) - u(k+i-1|k)
$$

Constraints on the output of the SGL and the states:  
\n
$$
y_{j,\min} \le y_j(k+i|k) \le y_{j,\max} \qquad j=1,2,\cdots,n_y, i=0,1,\dots,p
$$
\n(10)

$$
x_{j,\min} \le x_j (k+i|k) \le x_{j,\max} \qquad j=1,2,\cdots,n_x, i=0,1,\ldots,p \tag{11}
$$
#### 3.5 **The Standard Model Predictive Control (SMPC)**

The Standard Model Predictive Control (SMPC) is formulated based on the discrete state space model. Let the discrete state-space description of the uncertain SGL model in discrete time be given by [21]:

$$
x_m(k+1) = A_m(\theta)x_m(k) + B_w(\theta)u(k) + B_v(\theta)d(k)
$$
  
\n
$$
y(k) = C_m(\theta)x_m(k)
$$
\n(12)

$$
\begin{bmatrix} A_m(\theta) & B_m(\theta) \\ C_m(\theta) & 0 \end{bmatrix} \in \Omega, B_m(\theta) = \begin{bmatrix} B_w(\theta) & B_v(\theta) \end{bmatrix}
$$

where  $x_m(k) \in \mathbb{R}^{N_x}$   $u(k) \in \mathbb{R}^{N_y}$  and  $y(k) \in \mathbb{R}^{N_y}$ ,  $\forall k$  are the state, the input (feedwater flow rate) and output (SGL) respectively,  $d(k) \in \mathbb{R}^{N_d}$  is the external disturbance (steam flow rate),  $\Omega$  is some pre-specified set and  $\theta$  denotes the percentage of the power level (%FP) which determines the values of the SGL model parameters.  $A_m(\theta), B_w(\theta), B_v(\theta), C_m$  are power level dependent matrices in discrete time.

The SMPC changes its internal model, parameters and control settings according to the power level operations in order to stabilize the SGL by manipulating the feedwater flow rate while all the constraints are satisfied. The SMPC methodology is composed of three steps:

- i) future state/output prediction,
- ii) minimization of the desired cost function over the prediction horizon, and
- iii) implementation of the obtained optimal control input signal until the next sampling instant.

The control scheme uses the SGL model to predict the future response of the SGL. An optimization problem is solved to compute a sequence of *m* manipulated control signals *u* (*k* |*k*),  $u(k+1|k)$  ...  $u(k+m-1|k)$  for the *u*(*k* |*k*),  $u(k+1|k)$  ...  $u(k+m-1|k)$ for the SGL control. This is done by minimizing an appropriate cost function such that the  $p$  predicted outputs  $[y(k+1|k), y(k+2|k) \dots y(k+p|k)]$  follo follow the predefined trajectory.

The state-space description of the SGL model in discrete time is given by:  
\n
$$
\Delta x_m(k+1) = A_m(\theta) \Delta x_m(k) + B_w(\theta) \Delta u(k) + B_v(\theta) \Delta d(k)
$$
\n
$$
\Delta y(k) = C_m(\theta) \Delta x_m(k)
$$
\n
$$
\Delta x_m(k+1) = x_m(k+1) - x_m(k), \Delta x_m(k) = x_m(k) - x_m(k-1)
$$
\n(13)

The state-space discrete model in Eq. (13) is formulated into an augmented model by choosing a new state variable vector,  $[\Delta x_m(k) \quad y(k)]^T$ . The augmented model is given as follows [21]:

$$
\frac{x(k+1)}{\left[\Delta x_m(k+1)\right]} = \frac{A}{\left[A_m \quad 0\right]} \frac{x(k)}{\left[\Delta x_m(k)\right]} + \frac{B}{\left[B_w \quad B_v\right]} \left[\Delta u(k) \quad \Delta d(k)\right]^T,
$$
\n
$$
y(k) = \left[0 \quad 0 \quad 0 \quad 0 \quad 1\right] \left[\Delta x_m(k)\right],
$$
\n(14)

In the above definition of the SMPC methodology, the following can be noted:

- 1. The mass flow is balanced using feedback from state  $x_1(k) \approx G_1(q_w(k) - q_v(k))$
- 2. Swell/ shrink effects are minimized during different operation modes by using feedback from state  $x_2(k) \approx -\frac{62}{2}$ 2 2  $x_2(k) \approx -\frac{G_2}{\tau_2} (q_w(k) - q_v(k))$
- 3. Transient response is improved by using feedback from states  $(\tau_1^{-2} + 4\pi^2 T^{-2})$ Fransient response is improved by using<br>  $x_3(k) \approx G_3 q_w(k), x_4(k) \approx -(\tau_1^{-2} + 4\pi^2 T^{-2}) x_3(k)$
- 4. The SGL Model parameters vary as a function of the power level, and the SMPC uses power level dependent SGL model

5. Steady-state errors are minimized over the future horizon of  $p$ , and the size of the control move is minimized over the control horizon, *m,* by minimizing the cost function for augmented model  $J$  in Eqn. (21).

The SMPC uses a set of discrete Laguerre functions. The Laguerre function is used for its known ability to speed up the convergence of the control signal,  $\Delta u(k)$ , which enables the set point error  $e(k)$  to converge to zero. The core technique is to use additional tunable parameters  $\alpha$  (scaling factor for discrete-time Laguerre functions) and  $N$  (number of terms used in Laguerre function expansion), while optimizing the difference of  $\Delta u(k)$ .

Laguerre functions are expressed in a vector form as:

$$
L(k) = [l_1(k) \quad l_2(k) \quad . \quad . \quad l_N(k)]^T
$$

The set of discrete-time Laguerre functions satisfies the following difference equation:

$$
L(k+1) = H1L(k),
$$
\n<sup>(15)</sup>

where matrix  $H_l$  is  $N \times N$  and is a function of parameters a and  $\beta = (1 - a^2)$ . Initial condition is given by:

tion is given by:  
\n
$$
L(0)^{T} = \sqrt{\beta} [1 -a \ a^{2} -a^{3} \ \cdot \ \cdot \ \cdot (-1)^{N-1} a^{N-1}]
$$
\n(16)

$$
H_{l} = \begin{bmatrix} \alpha & 0 & 0 & 0 \\ \beta & \alpha & 0 & 0 \\ -\alpha\beta & \beta & \alpha & 0 \\ \alpha^{2}\beta & -\alpha\beta & \beta & \alpha \end{bmatrix}, L(0)^{T} = \sqrt{\beta} \begin{bmatrix} 1 & -\alpha & \alpha^{2} & -\alpha^{3} \end{bmatrix}^{T}
$$
(17)

Laguerre functions used in the SMPC methodology to compute a series of control signals:

$$
\Delta u(k_i + k) = \sum_{j=1}^{N} c_j(k_i) l_j(k_i) = L(k)^T \eta
$$
  

$$
\Delta u(k_i + k) = L(k)^T \eta
$$
 (18)

where  $\eta$  consists of N Laguerre coefficients:

$$
\eta = [c_1 \quad c_1 \quad . \quad . \quad . \quad c_N]^T,
$$

With initial state variable  $x(k)$ , the prediction of the future state variable,  $x(k+m|k)$ at sampling instant *m*, becomes:

$$
x(k+m|k) = A^{m}x(k) + \sum_{i=1}^{m-1} A^{m-i-1}BL(i)^{T} \eta
$$
 (19)

$$
x(k+m|k) = A^{m}x(k) + \phi(m)^{T} \eta, \quad \phi(m)^{T} = \sum_{i=1}^{\Delta} A^{m-i-1}BL(i)^{T}
$$
  

$$
y(k+m|k) = CA^{m}x(k) + \sum_{i=1}^{m-1} CA^{m-i-1}BL(i)^{T} \eta
$$
 (20)

The cost function of the SMPC plays an important role in the optimization phase. The cost function can be set out in various forms, but in general, the cost function is composed of the quadratic error between the future reference variable and the future controlled variable.

In this investigation, optimal control action by combining the constraints is found by minimizing the cost function for the augmented model *J* within the optimization window:

$$
J = (R_s - Y)^T (R_s - Y) + \Delta U^T R \Delta U, \qquad (21)
$$

which equivalent to:

$$
J = \sum_{i=1}^{p} x(k+i|k)^{T} Q_{SMPC} x(k+i|k) + \sum_{i=1}^{m} \Delta u(k+i)^{T} R \Delta u(k+i)
$$
 (22)

where:

$$
Y \cong [y(k_i + 1|k_i) \quad y(k_i + 2|k_i) \quad y(k_i + 3|k_i) \dots y(k_i + p|k_i)]^T
$$
  
\n
$$
\Delta U \cong [\Delta u(k_i) \quad \Delta u(k_i + 1) \quad \Delta u(k_i + 2) \dots \dots \dots \dots \quad \Delta u(k_i + m - 1)]^T
$$
\n
$$
R_s \cong [r_1 \quad r_2 \quad \dots \quad r_p]^T
$$
\n(23)

where  $\Delta u$  is sequence of control movement (manipulated signal), Y is predicted outputs (SGL) and  $R$  is the sequence of SGL set-point.

By substituting 
$$
x(k+m|k) = A^m x(k) + \phi(m)^T \eta
$$
 into cost function (22),  
\n
$$
J = \eta^T \left( \sum_{i=1}^p \phi(i) Q_{\text{SMPC}} \phi(i)^T + R \right) \eta + 2\eta^T \left( \sum_{i=1}^p \phi(i) Q_{\text{SMPC}} A^i \right) x(k_i)
$$
\n
$$
+ \sum_{i=1}^p x(k_i)^T (A^T)^i Q_{\text{SMPC}} A^i x(k_i)
$$
\n(24)

By minimizing cost function:

$$
\frac{\partial J}{\partial \eta} = 0 \Rightarrow
$$
\n
$$
\eta = -\left(\sum_{i=1}^{p} \phi(i) Q_{\text{SMPC}} \phi(i)^{T} + R\right)^{-1} \sum_{i=1}^{p} \phi(i) Q_{\text{SMPC}} A^{m} x(k_{i}), \eta = -\Omega^{-1} \psi x(k_{i}) \tag{25}
$$

$$
J_{\min} = x(k_i)^T \left( \sum_{i=1}^P (A^T)^i Q_{SMPC} A^i - \psi^T \Omega^{-1} \psi \right) x(k_i)
$$
 (26)

Minimized control signal is in the form of state feedback:

$$
\Delta U(k) = -K_{\text{SMPC}} x(k) \tag{27}
$$

$$
K_{SMPC} = L(0)^{T} \left( \left( \sum_{i=1}^{p} \phi(i) Q_{SMPC} \phi(i)^{T} + R \right)^{-1} \sum_{i=1}^{p} \phi(i) Q_{SMPC} A^{m} \right) = L(0)^{T} \Omega^{-1} \psi \tag{28}
$$

where  $Q_{\text{SMPC}}$  and *R* are weighting matrices. Both  $Q_{\text{SMPC}}$  and *R* are diagonal matrices with positive diagonal elements. By choosing the weight matrix  $Q_{\text{SMPC}} = C^T \times C$ , the error between the SGL set-point signal and the SGL output is minimized  $[21]$ .  *is a diagonal matrix with smaller components corresponding to* faster response. The choice of  $Q_{\text{SMPC}}$  and R may affect the location of the eigenvalues of the closed-loop system of the SGL, and may lead to the improved closed loop performance when using the augmented state-space model [21]. Once *QSMPC* and *R* are selected, the underlying optimal control trajectories are fixed. In general,  $\alpha$  is selected as an estimate of the real part (absolute value) of the closedloop dominant eigenvalue, dictated by  $Q_{\textit{SMPC}}$ , R and N, is increased until the control trajectory no longer changes with the increase of  $N(N)$  is the number of terms used in Laguerre function expansion). Therefore, these parameters affect the location of the eigenvalues of the closed-loop system, and in turn, affect the closed-loop control performance.

Asymptotic stability is established for the SMPC by using feedback control gains to compute parameter vector for the control sequence  $\Delta U(k)$  from states:

$$
\Delta U(k) = \Delta u_1(k) + \Delta u_2(k) + \Delta u_3(k) + \Delta u_4(k) + \Delta u_5(k)
$$
\n(29)

where

- $\triangleleft u_1(k) = -K_{x_1} \cdot \Delta x_1$ : minimizing mass balance
- $\Delta u_2(k) = -K_{X_2} \cdot \Delta x_2$ : minimizing swell and shrink effect
- $\Delta u_3(k) = -K_{X_3} \cdot \Delta x_3$  : minimizing FW flow effect
- $\Delta u_4(k) = -K_{X_4} \cdot \Delta x_4$ : minimizing FW flow effect
- $\triangleleft u_5(k) = -K_{X_5}$ .  $\triangle x_5$ : minimizing SGL error.

#### 3.6 **An Improved Model Predictive Control (IMPC)**

The Improved Model Predictive Control (IMPC) method has been formulated to investigate the potential performance improvement over SMPC by fine tuning the control sequence through assigning appropriate values in the weight matrix. The IMPC is essentially the SMPC, except that the matrix  $Q_{\text{SMPC}}$  is replaced by weight matrix  $Q_{\text{IMPC}}$ , where the elements of may have assigned with different values than the  $Q_{\textit{SMPC}}$  .

The matrix *QIMPC* is used to define the fine tuning parameter  $\alpha = [\alpha_1 \ \alpha_2 \ \alpha_3 \ \alpha_4 \ \alpha_5]$ , which modifies the manipulated control signal  $\Delta U(k)$ in IMPC as follows:

- $\Delta u_1(k) = -\alpha_1 K_{X_1} \cdot \Delta x_1$ : mass balance effect
- $\Delta u_2(k) = -\alpha_2 K_{x_2}$ .  $\Delta x_2$ : swell and shrink effect
- $\Delta u_3(k) = -\alpha_3 K_{X_3}$ .  $\Delta x_3$ : transient response during FW flow change
- $\Delta u_4(k) = -\alpha_4 K_{X_4}$ .  $\Delta x_4$ : transient response during FW flow change
- $\Delta u_5(k) = -\alpha_s K_{X_5}$ .  $\Delta x_5$ : SGL error

The idea of IMPC is to assign larger weights to aggressively encounter the effect of some of the salient characteristics of the SGL at different power levels. To illustrate, if mass balancing is important at certain power level, the value of the first element i.e.,  $Q(1,1)$  can be set to a larger value as a result  $\alpha_1 K_{X_1}$  increases so that higher weights can be given to  $\Delta u_1(k)$ . Larger weights can also be assigned to *Q*(2,2) for the swell-shrink effects.

For the simulation results presents in Section 4 and Section 5, the elements of  $Q_{\rm \scriptscriptstyle IMPC}$ at 5% power level are determined as follows:

The process starts by assigning an initial value of 0 to each of the diagonal element of *QIMPC* . Based on the characteristics of the SGL at 5%, the swell-shrink effect and the transient response have been identified as prominent factors affecting the control performance. To address these effects more aggressively, the values of *Q*(2,2) and *Q*(3,3) are set to 1.0. Note that these values are selected arbitrarily. The idea has been to investigate the potential performance improvement of SMPC through fine-tuning, not to optimize the  $Q_{\text{IMPC}}$  (which can be further explored). The value of *Q*(5,5) is set to 0.0001, as determined in the SMPC.

Using these assignment of values for  $Q_{\text{MPC}}$ , the value of  $J_{\text{min}}$  is computed by first computing  $\eta$ , and then  $J_{\text{min}}$  as follows (note that any change in  $Q_{\text{IMPC}}$  affects  $\eta, \Omega, \psi$ , which in turn may affect the value of  $J_{\min}$ ):

$$
\frac{\partial J}{\partial \eta} = 0 \Rightarrow
$$

$$
= 0 \Rightarrow
$$
  

$$
\eta = -(\sum_{i=1}^{p} \phi(i)Q_{\text{IMPC}}\phi(i)^{T} + R)^{-1} \sum_{i=1}^{p} \phi(i)Q_{\text{IMPC}}A^{m}x(k_{i}), \eta = -\Omega^{-1}\psi x(k_{i})
$$
(30)

$$
J_{\min} = x(k_i)^T \left( \sum_{i=1}^P (A^T)^i Q_{MPC} A^i - \psi^T \Omega^{-1} \psi \right) x(k_i)
$$
 (31)

This value of  $J_{\text{min}}$  is recorded. This process is then repeated and the  $J_{\text{min}}$  values are computed and recorded by changing the value of  $Q(1,1)$ ,  $Q(4,4)$  and  $Q(5,5)$ , one at a time, while keeping the values of  $Q(2,2)$  and  $Q(3,3)$  fixed. The values of  $Q(1,1)$ ,  $Q(4,4)$  and  $Q(5,5)$  are changed as follows:

- $Q(1,1)$ : from 0.0 to 1.0 with an step increment of 0.1.
- $\bullet$   $Q(4,4)$ : from 0.0 to 0.01 with an step increment of 0.001
- $\bullet$  *Q*(5,5): from 0.0001 to 0.01 with an step increment of 0.0001

Finally, the combination of the element values that gives the lowest  $J_{\min}$  from all these runs has been taken as the initial  $Q_{\text{IMPC}}$ . The  $J_{\text{min}}$  with some sample value assignments for the elements of initial  $Q_{\text{IMPC}}$  at 5% PL is shown in Table 3.

In the table, the combination of values in the  $5<sup>th</sup>$  row gives the smallest  $J_{\min}$ , and hence, selected as the initial  $Q_{\text{IMPC}}$ . Finally, using this  $Q_{\text{IMPC}}$ , a number of test cases are simulated, and the different element values are manually adjusted (if required) to determine the final  $Q_{\text{IMPC}}$ . The performance of the IMPC has been evaluated on the basis of the performance measures, presented in Section 4, for this purpose.

$Q_{IMPC}$ diagonal elements					$J_{\min}$	<b>Remark</b>
(l, l)	(2,2)	(3,3)	(4,4)	(5,5)		
0.2	1	$\mathbf{1}$	0.001	0.001	8.40375E-05	
$\theta$	$\mathbf{1}$	$\mathbf{1}$	0.006	0.001	5.06493E-05	
0.3	$\mathbf{1}$	$\mathbf{1}$	0.001	0.008	0.014166174	
0.2	1	$\mathbf{1}$	0.01	0.006	0.007655725	
0.1	$\mathbf{1}$	$\mathbf{1}$	0.005	0.001	3.98695E-05	Smallest $J_{\min}$
0.3	1	$\mathbf{1}$	0.002	0.001	0.000110967	
0.4	1	$\mathbf{1}$	$\theta$	0.001	0.000192181	

Table 3 An example of computing  $Q_{\rm \scriptscriptstyle IMPC}$  at 5% PL

Once the  $Q_{\text{IMPC}}$  is determined, the IMPC feed-back gain is computed as follows:

Once the 
$$
Q_{IMPC}
$$
 is determined, the IMPC feed-back gain is computed as follows:  
\n
$$
K_{SMPC} = L(0)^T \left( \left( \sum_{i=1}^p \phi(i) Q_{IMPC} \phi(i)^T + R \right)^{-1} \sum_{i=1}^p \phi(i) Q_{IMPC} A^m \right) = L(0)^T \Omega^{-1} \psi
$$
\n(32)

As mentioned above, the IMPC has been formulated and evaluated only to study the effect of assigning certain weights to different states, represented in the five elements of the  $Q_{\text{IMPC}}$  matrix. Clearly, the values selected for  $Q_{\text{IMPC}}$  in this study may not be optimal. Other  $Q_{IMPC}$  values (based on the power level) may lead to greater demonstrations of the effects of these parameters on the MPC based SGLC systems. However, this has been left as a future work.

## 3.7 **Summary**

In this section, the fundamentals of the MPC, and the model linearization have been discussed, and the formulations of the SMPC and the IMPC methodologies have been presented. The SMPC has been formulated using existing advanced MPC methodologies. The IMPC has been developed to investigate the performance of a MPC based approach for the SGL control systems that takes into account the effect of mass balance, transient response and swell and shrink effects, in addition to steady-state errors by manipulating the values of the weight matrix  $Q_{\text{IMPC}}$  A heuristic approach used in this study to compute  $Q_{\text{IMPC}}$  for simulation has also been discussed.

# 4 **Simulation Studies**

## 4.1 **Background and objectives**

The performance of the SMPC and the IMPC have been evaluated under the different operating conditions through computer simulation. In this section, the results are presented and discussed.

Simulation results are analyzed for several performance measures that include i) set-point tracking, ii) load following subject to reactor power change in steps and in ramps, iii) load rejection, and iv) performance under flow disturbances and signal noise.

To compare the SMPC and the IMPC performance with conventional PI controls, a fine-tuned PI controller is also implemented in Matlab-Simulink environment. The parameters  $K_p$  and  $K_i$  of the PI controller are fine-tuned at each of the five power level regions, given in Table 2. Matlab-Simulink tool has been used for finetuning the PI parameters by measuring and observing major performance for step responses such as overshoot, undershoot, settling time and steady-state errors.

# 4.2 **Simulation set up**

The Irving model, discussed in Section 3.2, has been used for the computer simulation. The simulation has been carried out a Matlab-Simulink environment. The linear parameter varying model, discussed in Section 3.3, has been used for the SGL. The power level dependent parameters (given in Table 1) have been used over the five power level regions, given in Table 2. Sampling time has been set to 1 sec [22].

For all the computer simulation (also for physical experiments presented in Chapter 5), constraints have been applied to the allowable FWF rates. The values of the FWF rate have been constrained within the range  $0 \le q_w \le 2500 \text{ kg/s}$ . These constraints enforce that the FWF rate cannot be negative, and cannot be over 2,500 kg/s. This has been done to account for the capacity of the FWCV in existing NPPs. Furthermore, the SGL upper and lower limit constraints have also been imposed. The specific values for these limits have been set in the formulation based on the power level. The values for  $\alpha$  and  $N$  for Laguerre functions have been selected as  $\alpha$  =0.95 and  $N = 4$ , based on the location of the desired eigenvalues.

#### 4.2.1 **Simulation of the SGL**

The simulation set up for the control schemes is shown in a block diagram in Fig. 6, where PL indicates the reactor power level.

In Fig. 6, the control signals are indicated as UPI, USMPC and UIMPC for PI, SMPC and IMPC control strategies, respectively. The figure also shows that the UIMPC control signals are sent to the feed-water control valve (indicated as FWCV) of the SG. The feed-water flow and the steam flow have been indicated as U and SF, respectively. The point where steam flow disturbance is introduced in the simulation is indicated as SFd, and the point where both feed-water flow disturbance and signal noise are introduced is indicated as Ud in the figure.

Identical FWCVs and SGs have been used for the PI and the SMPC schemes (not shown in the figure). The details of the IMPC simulation setup is shown in the block diagram at the lower part of Fig. 6.

## 4.2.2 **State observer**

The SMPC and the IMPC schemes have used an observer for state estimation. The observer has been constructed using the equation:

$$
\hat{x}(k+1) = A \hat{x}(k) + Bu(k) + L_{ob}(y(k) - C \hat{x}(k))
$$
\n(33)  
\n
$$
\Delta U(k) = K_{y}.e(k) - K_{x}.\Delta \hat{x}(k)
$$
\n(34)  
\n
$$
e(k) = r(k) - y(k)
$$

Observer eigenvalue placement is similar to the controller eigenvalue. Observer gain vector  $L_{ob}$  is computed based on the desired closed-loop characteristics. For example, the observer gain vector  $L_{ob}$  used for the IMPC and the SMPC schemes at 5% power level have been computed as follows:

- SMPC:  $L_{ob}$ =[0.8511 -0.1998 -0.2081 -5.0706]; eigenvalue [.85 .75 .90 .95]
- IMPC:  $L_{ob}$  = [2.0427 -0.5985 -0.8510 -3.0111]; eigenvalue [.80 .70 .85 .95]



**Fig. 6 Block diagram for PI, SMPC and IMPC**

### 4.2.3 **Selection of simulation scenarios**

The simulation scenarios are specifically designed to investigate/study the performance of the MPC based approaches, and to compare with conventional PI control strategies. Simulation are carried out to investigate the performance of the control strategies under the following input and disturbances conditions:

- Step response under different operating conditions
- Set point tracking
- Load following subject to power level change in steps
- Load following subject to power level change in ramp
- Load rejection
- Performance subject to FWF disturbance in steps
- Performance subject to SF disturbance in steps
- Performance subject to random noise in FWF signal

All simulation studies are focused on the response of the control strategies in transient and steady state conditions. In the following, the simulation results are discussed.

# 4.2.4 **Step responses**

The step responses at 5%, 15%, 30%, 50% and 100% power levels are shown in Figs.7 to Figs. 16. For this set of simulation, the set point at each power level has been step up by 100 centimeters, which is 10% of the full range that has been assumed to be 1 meter. In all these figures, the unit of  $\triangle SGL$  is given in centimeters, and the control signal, which is the FWF rate, is given in kg/s.

The SGLs with SMPC, IMPC and PI controllers at 5% power level are shown in Fig. 7, and the respective control signals are shown in Fig. 8. The simulation time has been set to  $10x10^4$  mSec (Fig. 7) for this simulation to demonstrate that the SGL with PI converges to zero. However, it has been observed for all simulation in this section that the SGL with the SMPC and the IMPC converge to zero much earlier than that. Furthermore, setting time  $(+/- 2\%)$  for all control strategies is much less than  $10x10<sup>4</sup>$  mSec. Therefore, the rest of the figures presented in this section will show the simulation results up to  $2x10<sup>4</sup>$  mSec. It is further noted that all the steady-state errors reported in this study are the errors at  $2x10^4$  mSec.

From Fig. 7, it can be seen that there is no overshoot with either the SMPC or the IMPC scheme, while there is 20% overshoot with the PI. The IMPC has the least undershoot (20%), followed by the PI (28%). The SMPC has the largest undershoot (45%). Both IMPC and SMPC have a settling time 5000 mSec, which is 1000 mSec less than the PI (6000 mSec).



**Fig. 7 SGL subject to a step change at PL=5%**



**Fig. 8 Control signal subject to a step change at PL=5%**

Eigenvalues of the IMPC and the SMPC control strategies at PL=5% are shown in Table 4, and the state feedback gains are shown in Table 5. From Table 4, it can be observed that the locations of the eigenvalues for these control strategies are inside the unit circle, ensuring that all control systems are stable.

<b>Control</b>	<b>Closed-Loop Eigenvalues</b>								
$\mathcal{Q}_{\textit{SMPC}}$	0.8246	$0.9468 + j0.0508$	$0.9468 - j 0.0508$	$0.9885 + j 0.0055$	$0.9885 - j0.0055$				
$Q_{\text{IMPC}}$	0.8113	$0.9540 + j 0.0568$	$0.9540 - i 0.0568$	$0.9880 + j 0.0049$	0.9880- $j$ 0.0049				

**Table 4 The Eigenvalues for IMPC and SMPC at PL=5%**

	<b>Feedback Gain</b> ( $K_{mpc}$ )								
Control	$K_{1}$	$K_{2}$	$K_{3}$	$K_4$	$K_{5}$				
<b>SMPC</b>	1.8685	0.1432	0.2863	0.0108	0.0080				
<b>IMPC</b> 2.0583		0.1571	0.2428	0.0053	0.0089				

**Table 5 Feedback gains for IMPC and SMPC at PL=5%**

The SGL and control signals with 15%, 30%, 50% and 100% power levels with respect to step response are shown in Fig. 9 to Fig. 16. The main observations from this set of simulation are summarized in Table 6 along with a discussion, presented later in this section.



**Fig. 9 SGL subject to a step change at PL=15%**



**Fig. 10 Control signal subject to a step change at PL=15%**



**Fig. 11 SGL subject to a step change at PL=30%**



**Fig. 12 Control signal subject to a step change at PL=30%**



**Fig. 13 SGL subject to a step change at PL=50%**



**Fig. 14 Control signal subject to a step change at PL=50%**



**Fig. 15 SGL subject to a step change at PL=100%**



**Fig. 16 Control signal subject to a step change at PL=100%**

The performance of the IMPC, the SMPC and the PI algorithms in terms of four major performance measures (overshoot, undershoot, settling time and steady-state errors) are shown in Table 6. From the table, it can be seen that both SMPC and IMPC can achieve zero steady state errors for all power levels within the simulation time  $(2x10<sup>4</sup> \text{ m}$ Sec), whereas PI may have small errors in low power ranges. The IMPC has shown less undershoot than PI and SMPC. The SMPC and the IMPC can achieve zero overshoot, while relatively larger overshoot with PI can be observed, particularly at low power operations. These simulation results demonstrate the challenges of constant gain conventional PI controllers to control the SGL over full power ranges that include start-up and low power operations. This also indicates that the MPC based approaches may be a feasible methodology to control a SGL in all power levels.

%PL		Over Shoot $(\% )$		Undershoot $(\% )$		<b>Settling Time (mSec)</b>			<b>Steady State Error at</b> $T = 2x10^4($ %)			
	<b>IMPC</b>	<b>SMPC</b>	PI	<b>IMPC</b>	<b>SMPC</b>	PI	<b>IMPC</b>	<b>SMPC</b>	PI	<b>IMPC</b>	<b>SMPC</b>	<b>PI</b>
5	$\Omega$	$\Omega$	20	20	45	28	5000	5000	6000	$\Omega$	$\Omega$	2.70
15	$\Omega$	$\theta$	16	20	60	22	2000	1500	5000	$\Omega$	$\mathbf{0}$	2.5
30	$\Omega$	$\overline{0}$	15	10	80	50	1000	1000	2000	$\Omega$	$\theta$	
50	$\Omega$	$\overline{0}$	15	5	50	30	800	500	2000	$\Omega$	$\theta$	$\overline{0}$
100	$\Omega$	$\overline{0}$	3	$\Omega$	$\Omega$	$\theta$	411	380	1200	$\Omega$	$\Omega$	

**Table 6 Performance of IMPC, SMPC and PI strategies**

## 4.2.5 **SGL subject to step changes in reactor power level**

This simulation has been carried out in order to study the performance of the control strategies when the reactor power level is changed from 5% to 22% in steps. The power level is increased as follows: i) from 5% to 10%, PL is increased by a step of  $1\%$ ; ii) from  $10\%$  to  $14\%$ , PL increased by a step of  $2\%$ ; and iii) from  $14\%$  to 20%, PL increased by a step of 3%. Finally, the PL is increased by 2% to arrive at 22%. The results are shown in Fig. 17 and Fig. 18 (SGL and control signal, respectively).

Visual inspection of Fig. 17 will reveal that the settling time for the PI is much larger than both MPC based approaches for more than 8% PL. Both SMPC and IMPC have shown consistent ability for fast set point tracking, which is not necessarily the case for the PI. No overshoots have been observed for any of the MPC based strategies at any power level. Undershoots of the SMPC is a little higher than the PI for more than 17% PLs. Based on these observations, the IMPC can be seen as the best performing control strategy in terms of settling time, overshoot/undershoot, steady state error and the transient responses.



**Fig. 17 SGL subject to multiple PL step-up changes from 5% to 22%** 



**Fig. 18 Control signal subject to multiple PL step-up changes from 5% to** 

### 4.2.6 **SGL response subject to ramp change in reactor power**

This simulation has been carried out to investigate the performance of the control strategies under changes in power level, when the changes are made in ramp (which is usually the preferred method in real power plants while the power level is increased).

For this simulation, the reactor is powered up continuously from 5% to 100% (ramped up), and then powered down to 5% (load rejection). The results are shown in Fig. 19 and Fig. 20 (the SGL and the control signal, respectively).

For this simulation, an advance PI Simulink block with bump-less transfer capability has been used. Five different fine-tuned PI controllers for five different power level dependent SG Models have been employed.

It can be seen from Fig. 19 that although IMPC and SMPC schemes have consistently slightly outperform the PI in terms of set-point tracking and transient responses; however, in general, the performance of all three control strategies are close and comparable when multiple PI controllers are used in bump-less output.



**Fig. 19 SGL subject to power level changes from 5 % to 100 %, followed by a load rejection to 5%**



**Fig. 20 Control signal subject to power level changes from 5 % to 100 % followed by a load rejection to 5%**

# 4.2.7 **SGL response subject to steam flow disturbance**

Steam flow disturbance is one of the main disturbances for the SGL during different operating modes of a power plant. In this section, the performance of all three control strategies under steam flow disturbance are compared. For this set of simulation, 5% and 50% power levels are considered, to evaluate the performance in lower and higher power levels, respectively. In the simulation, disturbance (SFd in Fig. 6 was applied in the steam flow by introducing a step up, and a step down signal with the SF signal.

The SGL control performance of SMPC, IMPC and PI controllers at 5% power level are shown in Fig. 21, and the respective control signals are shown in Fig. 22. From Fig. 21, it is clear that both IMPC and SMPC have been able to reject the effect of SF disturbance on the SGL effectively in about 3 secs after the step-up disturbance injection. The PI can be seen as unable to reject the disturbance effect even until 15 secs after the step-up disturbance injection. Furthermore, the SMPC sends larger control signals (Fig. 22) as compared to the IMPC and the PI. This may indicate greater efforts by the control valve with SMPC. The magnitude of the control signals for the IMPC and the PI are comparable. Based on the above observations, it appears that the IMPC can provide better SF disturbance effect rejection capability.

The SGL control performance of SMPC, IMPC and PI controllers at 50% power level are shown in Fig. 23, and the respective control signals are shown in Fig. 24. As shown in Fig. 23, the IMPC and the SMPC controls have again shown better performance for disturbance effect rejection much earlier than the PI. The PI has also been able to reject the disturbance effect at this power level, but not as quickly as the SMPC and the IMPC. It is noted that SMPC has even smaller overshoot/undershoot, and required less control action than IMPC in this particular case. However, it may also be noted that the  $Q_{IMPC}$  matrix used in all simulation is tuned for 5% power level. More appropriate selection of weights in  $Q_{\text{IMPC}}$ , based on different power level, may lead to further improvement of its performance, and can be further investigated.

From the simulation results at 5% and 50% PL, it can be seen that disturbance effect rejection by PI control at 5% PL is much worse than that at 50% PL. This again demonstrates that the SGL control is more challenging at low power operations. Note that PI controller parameters are fine-tuned using Matlab Simulink tuning tool.



**Fig. 21 SGL subject to a SF disturbance at PL=5%**



**Fig. 22 Control signal subject to a SF disturbance at PL=5%**



**Fig. 23 SGL subject to a SF disturbance at PL=50%**



**Fig. 24 Control signal subject to a SF disturbance at PL=50%**

#### 4.2.8 **SGL response subject to feed-water flow disturbance**

Feed-water flow disturbances in the process may be introduced in different forms such as transmitter failures and FWCV unintentional opening/closing. In this section, the performance of all three control strategies under feed-water flow disturbances are compared. For this set of simulation, 5% and 50% power levels are considered to represent the lower and the higher power levels, respectively. In these simulation, disturbance has been applied in the feed-water flow by introducing a step up, and a step down signal with the feed-water flow signal (Ud in Fig. 6).

The SGL control performance and control signals of SMPC, IMPC and PI controllers at 5% power level are shown in Fig. 25 and Fig. 26, respectively, and those at 50% PL are shown in Fig. 27 and Fig. 28, respectively. The relative SGL control performance of the control strategies for FWF disturbance effect rejection at 5% and 50% PLs are similar to the results presented in Section 4.2.7, and hence, detail discussion is omitted for the shake of brevity.



**Fig. 25 SGL signal subject to FWF step-disturbances at PL=5%**



**Fig. 26 Control signal subject to FWF step-disturbances at PL=5%**



**Fig. 27 SGL subject to FWF step-disturbances at PL=50%**



**Fig. 28 Control signal subject to FWF step-disturbances at PL=50%**

## 4.2.9 **SGL response subject to random measurement noise in the FWF**

Random noise disturbance in feed-water flow signal can be caused by several factors such as poor grounding, bad connection, or Electro-Magnetic Interference (EMI) from a plant environment. In this section the performance of all three control strategies are compared under random noise-disturbance in the feed-water flow. As for other simulation under disturbances, 5% and 50% power levels are considered. Random noise signal has been generated by using Simulink block. The amplitude for the random signal is selected as 0.3. The noise signal is introduced in feed-water flow signal (Ud in Fig. 6).

The SGL control performance of SMPC, IMPC and PI controllers at 5% power levels are shown in Fig. 29, and the respective control signals are shown in Fig. 30. As shown Fig. 29, random noise has caused about +/- 4% oscillation on the SGL for the PI controller. The IMPC and the SMPC have been able to handle the noise effect more resiliently, with approximately +/- 0.4% oscillation on the SGL. The

SMPC needed relatively larger control action than the other two strategies, as shown in Fig 30.

The SGL at the 50% power level is shown in Fig. 31, and the respective control signals are shown in Fig. 32. For the 50% PL, the random noise disturbance rejection performance (in terms of SGL oscillation) for all three control strategies are close to each other, and much better than their respective performance at the 5% PL (Fig. 31). Once again, this outcome demonstrates that increasing the power level reduces the effect of the random noise disturbance on SGL. Note that at 50% PL, the SGL with the SMPC has been found to be noisier than both IMPC and PI.



**Fig. 29 SGL subject to FWF random noise disturbance at PL=5%**



**Fig. 30 Control signal subject to FWF random noise disturbance at PL=5%**



**Fig. 31 SGL subject to FWF random noise disturbance at PL=50%**



**Fig. 32 Control signal subject to FWF random noise-disturbance at PL=50%**

# 4.3 **Summary**

The performance of the SMPC and the IMPC based control strategies has been investigated, and compared with an optimized PI based controller through computer simulation. The control performance has been evaluated mainly in four performance measures: i) overshoot, ii) undershoot, iii) settling time, and iv) steady state errors. Simulation scenarios have been specifically selected in order to investigate the performance for set point tracking, load following (in step and programed ramp), load rejection, and to see how they would perform under disturbances and signal noises in the SF and the feed-water flow.

# 5 **Physical Test Results on the PLS**

## 5.1 **Background and objectives**

Testing control systems in a physical environment is important to verify and validate the performance and limitations of a control strategy. The quality and accuracy of the test is dependent on the physical system with respect to actual system dynamics. In this section, a physical test bench consisting of a mock-up SG system, referred to as the Plate-Level System (PLS), is used to study the performance of all three control strategies. The idea has been to investigate the effectiveness of the control strategies on a realistic system. A subset of the computer simulation studies has been selected for the PLS test. For the analysis of the PLS test results, emphasis has been put on the similarity and the differences of relative performance trends of the PLS test results to that of the corresponding computer simulation.

## 5.2 **Physical simulation set up**

The PLS used to mimic a realistic steam generator level in CIES lab is illustrated in Fig. 33, and a schematic diagram is shown in Fig. 34. As shown in Fig. 34, the PLS system consists of a cylindrical tank containing an aluminum plate which can be controlled vertically by manipulating the position of the valve. This valve position changes the air flow-rate, which in turn changes the plate level. The plate moves within an admissible range of 0-20 cm. Plate level "SGL" is measured by a laser level sensor installed at the top of the tank (Fig. 33), which passes this information in the form of 4-20 mA output signals to an I/V converter (Fig. 33). The voltage signal from the converter is then passed to a data acquisition (DAQ) system. A DT9812 Series DAQ module has been used that supports eight singleended analog input channels, two analog output channels (DAC0 and DAC1), eight fixed digital input lines, and eight fixed digital output lines. This DAQ interfaces with the MATLAB Data Acquisition (DAQ) subsystem. The FWF and SF signals, as determined by the control strategy, are passed from the MATLAB DAQ to DT9812 DAQ over the channels DAC0 and DAC1. These signals then go to the



**Fig. 33 The Plate Level System (PLS)**

A schematic diagram of the plate-level system used for physical simulation is shown in Fig. 34. [23]


**Fig. 34 A schematic diagram of the PLS with a digital filter for simulating non-minimum phase characteristics**

## 5.3 **Selection of simulation scenarios**

The simulation scenarios for the PLS tests are kept similar to the computer simulation (discussed in Section 4.2), so that meaningful comparisons can be made. The results of the simulation are discussed in the following.

Note that the PLS cannot be pulled-down by the feed-air valve during the set point step-up change, and hence, undershoot performance subject to set point step-up change cannot be measured for PLS test studies. Therefore, undershoot measure during set point step-up change has been disregarded for all test results presented in this section. Furthermore, the PLS tests with SF disturbance have not been performed, as the SF valve on the PLS is not physically integrated with the process. Furthermore, only random noise disturbance in the FWF has been considered for physical tests.

### 5.3.1 **Step response**

The step responses of the control strategies on the PLS are investigated at 5%, 15%, and 100% power levels. These power levels are selected to reflect the performance evaluation of the control strategies at low power levels and a high power level. The results are shown in Fig. 35 to Fig. 40. As in the computer simulation, the unit of  $\triangle SGL$  (change in SGL) is given in centimeters, and the control signal, which is the FWF rate, is given in kg/s. The main observations from this set of simulation have been summarized in Table 7, along with a discussion, to be presented later in this section. The simulation time has been set to  $3.5x10<sup>4</sup>$ . The longer simulation time (than the respective computer simulation) has been used to ensure appropriate settling time (+/- 2% SGL) for all of the control strategies. The steady state errors reported in this section are the error at the end of the simulation times.

The SGL performance of SMPC, IMPC and PI controllers at 5% power level are shown in Fig. 35, and the respective control signals are shown in Fig. 36. As shown in Fig. 35 (and Table 7), only a little overshoot has been observed for the IMPC and the SMPC schemes at this PL (1.7% and 4.56%, respectively). There were zero overshoots with these controllers in the computer simulation at 5% PL (Table 6). However, the overshoot with the PI on the PLS is about 33% (computer simulation for PI has been 19.1%). This may be due to the saturation of the PI control signals, as shown in Fig. 36.

In summary, the relative SGL performance *trend* of the controllers on the PLS, in terms of overshoot, is reasonably close to that of the computer simulation.

The steady state errors on the PLS for IMPC, SMPC and PI in Fig. 35 have been 0.5%, 0.3%, and 3.25%, respectively (Table 7). IMPC and SMPC have zero steady state errors in computer simulation (Table 6). And therefore, relative SGL performance trend of the controllers on the PLS and the computer simulation, in terms of steady state error, is also fairly close. The PI needed relatively larger control action than the other two strategies, as shown in Fig 36.

At 5% power level, both SGL and control signals are found to be noisy as shown in Fig. 36. And hence, the settling time cannot be clearly identified. These noises are relatively more as compared to the corresponding computer simulation. However, this can be expected due to the physical nature of the test, and the characteristics of the PLS. Furthermore, although the PLS closely mimic the Irving model, some model mismatch can be expected, which may lead to a variation in the performance of the MPC based control strategies. It is noted that such noises in the SGL and the control signals have been observed in all test cases in low power levels due to the possible reasons discussed above.



**Fig. 35 SGL of the PLS at PL=5%**



**Fig. 36 Control signal to the PLS at PL=5%**

The SGL performance of SMPC, IMPC and PI controllers at 15% power level in shown in Fig. 37, and the respective control signals are shown in Fig. 38. Visual inspection of Fig. 37 clearly reveals that SGL by the SMPC and the PI have suffered from oscillations. This is different from the corresponding computer simulation, as no oscillation has been observed (see Fig. 7). This may have occurred due to model mismatch. The IMPC has shown no SGL oscillation on PLS, possibly indicating that the IMPC is more robust in terms of model mismatch.

The PI has shown a larger overshoot of 32.23% (see Table 7) than the computer simulation (11.08%, see Table 6). The SMPC has shown 13.33%% overshoot, whereas, the IMPC has only a little overshoot (3.33%). Both IMPC and SMPC overshoots were zero in the computer simulation. Therefore, the IMPC has again shown better capability in terms of overshoot.

The steady state errors on the PLS, for all controllers, are comparable to that of the computer simulation (see Table 6 and Table 7). For the settling time, all control strategies took longer (about 6000 mSec) on the PLS than corresponding computer simulation; however, the relative time difference among the control strategies between the PLS and the computer simulation is not significant (see Table 6 and Table 7).



**Fig. 37 SGL of the PLS at PL=15%**



**Fig. 38 Control signal to the PLS at PL=15%**

The SGL performance of SMPC, IMPC and PI controllers at 100% power level are shown in Fig. 39, and the respective control signals are shown in Fig. 40.

From Fig. 39, the SGL performance at 100% power can be seen as similar to that of the PLS simulation at 15% (Fig. 37).



**Fig. 39 SGL of the PLS at PL=100%**



**Fig. 40 Control signal to the PLS at PL=100%**

The performance of the three control strategies for the physical simulation is summarized in Table 7. From this table, it can be seen that the relative performance trends of the control strategies are close to those in the computer simulation, except for the settling times, where the PLS tests have required larger settling times for all control strategies (see Tables 6 and 7). Furthermore, overshoots can be seen in both MPC based approaches for PLS tests, although the overshoot is minimal for the IMPC scheme. Steady state error for all three control strategies on the PLS are also close to that of the computer simulation.

%PL	Over Shoot $(\%)$			Settling Time (mSec)			Steady State Error (%) at simulation end time		
	<b>IMPC</b>	<b>SMPC</b>	PI	<b>IMPC</b>	<b>SMPC</b>	<b>PI</b>	<b>IMPC</b>	<b>SMPC</b>	<b>PI</b>
	1.7	4.56	33.33	na	na	na	$\theta$	0	3.25
15	3.33	13.33	32.23	6760	6600	7050	$\theta$	1.17	$\mathcal{D}_{\mathcal{L}}$
100	1.3	10.66	31.02	7460	4000	5200	$\theta$	$\theta$	0

**Table 7 Performance of IMPC, SMPC and PI strategies on the PLS**

### 5.3.2 **SGL response subject to changes in reactor power level in step**

The same as in the computer simulation presented in Section 4.2.5, this PLS test has been done in order to study the performance of the control strategies when reactor power levels are changed from 5% to 22%. From 5% to 19%, PL has been increased by a step of 2%; and then, the PL is increased by 3% to arrive at 22%. The results are shown in Fig. 41 and Fig. 42 (the SGL and the control signals, respectively).

It can be seen in Fig. 41 that the load following capability of the IMPC and the SMPC controllers are better than the PI, and close to each other. However, their performance is a little noisy compared to the corresponding computer simulation (Fig. 17), most likely due to the model mismatch. Comparing Fig. 41 and Fig. 17,

it is reasonable to conclude that the performance trends, shown in the PLS tests and the computer simulation in terms of load following are close to each other.



**Fig. 41 SGL of the PLS subject to PL step up changes from PL=5% to 22% followed by a load rejection to PL=5%**



**Fig. 42 Control signal to the PLS subject to PL step up changes from PL=5% to 22% followed by a load rejection to PL=5%**

### 5.3.3 **SGL response subject to changes in reactor power level in ramp**

For this PLS test, the reactor power is increased continuously from 5% to 100% (ramp up), and then reduced to 22% (load rejection). The results are shown in Fig. 43 and Fig. 44 (SGL and control signal, respectively). In this simulation, the set point tracking performance of all three control strategies have shown little degradation compared to their computer simulation counterparts (Fig. 19). One of the major reasons is the possible model mismatch.

The SMPC has the best performance in terms of set point tracking and load following, with IMPC a close second. The IMPC, however, has the least undershoots, and also the least settling time (after load rejection). Relatively much larger overshoot/undershoot and settling time can be noted for PI.

Note that the spikes in the control signal in PI are due to the switch of the controller to a different power level. This can be avoided by using bump less PI as shown in corresponding computer simulation (Fig. 20).



**Fig. 43 SGL of the PLS for PL ramp up changes from PL=5% to 80% followed by load rejection to PL=10%**



**Fig. 44 Control signal to the PLS for PL ramp up changes from PL=5% to 80% followed by load rejection to PL=10%**

## 5.3.4 **SGL response subject to random noise in the FWF measurements**

This section presents the performance of control strategies subject to random noise in the FWF measurements. For this set of the PLS tests, 5% and 50% power levels are considered, as in the computer simulation.

The results at 5% PL are shown in Fig. 45 and Fig. 46 .. Little more noises and oscillations in the SGL can be seen for all control strategies in Fig. 45, as compared to the respective computer simulation, Fig. 29 (possibly, due to model mismatch). The performance in terms of noise effect rejection of all control strategies are comparable.



**Fig. 45 SGL of the PLS subject to FWF random noise at PL 5%**



**Fig. 46 Control signal to the PLS subject to FWF random noise at PL 5%**

The results at 50% PL are shown in Fig. 47 and Fig. 48. At this power level, the noise effect rejection performance of all control strategies are comparable, and similar to that of the respective computer simulation (Fig. 31).



**Fig. 47 SGL of the PLS subject to FWF random noise at PL 50%**



**Fig. 48 Control signal to the PLS subject to FWF random noise at PL 50%**

# 5.4 **Summary**

The performance of the MPC based controllers has been evaluated through a set of physical tests on the PLS. The performance measures of the control strategies are evaluated in terms of set point tracking, load following in steps and programed ramp, load rejection, and flow disturbance and signal noise rejection capabilities. The performance measures of the control strategies on the PLS are compared with the computer simulation results.

## 6 **Conclusions and Future Work**

### 6.1 **Contributions**

The performance of the MPC based strategies to control the SGL in NPPs have been evaluated. In-depth studies have been performed to better understand the capability of the MPC based control schemes to deal with the challenges in the SGL control in NPPs over the full power range. Performance has been evaluated with respect to all operating and transient conditions of a SG in a NPP.

These evaluations have been carried out using a linearized steam generator dynamic model. The MPC controllers used are based on existing methodologies. Furthermore, any potential performance improvement through fine-tuning of some of the control parameters (based on the dynamic characteristics of the SGL) has also been investigated.

For performance evaluation, two versions of the MPC strategy, the SMPC and the IMPC, have been designed and simulated. The SMPC scheme is based on existing MPC methodologies. The IMPC has been examined for potential performance improvement over SMPC by selecting appropriate values in the weight matrix of the objective function.

The Irving model has been used as the underlying dynamic model of the SG in this study. This model has been linearized over the entire power range. Since the Irving model changes with power levels, power level dependent SGL parameters of the SGL have been designed. Power level dependent control parameters have been designed through minimizing an appropriate cost function that has been selected. Furthermore, for the IMPC, a simple strategy has been presented to compute the weights in the  $Q_{IMPC}$  matrix. The  $Q_{IMPC}$  matrix has been used to manipulate the control signals in order to improve the SGL performance of the MPC based strategies.

Performance of the SMPC and the IMPC has been evaluated, and compared with an optimized PI controller. The performance has been evaluated through computer simulation, and also through a set of physical tests on the PLS (the mock-up steam generator level system). Performance evaluations have been done in terms of i) set point tracking, ii) load-following, transient responses, and iii) effectiveness under flow disturbances and signal noise.

### 6.2 **Discussions and conclusions**

In the computer simulation, the SMPC and the IMPC schemes have shown zero overshoot and steady-state errors over all power levels, for the SGL subject to the step response. In the PLS tests, the IMPC scheme has shown zero steady-state errors and close-to-zero overshoots, while the SMPC has shown a little more overshoots (others are close-to-zero). There are no significant differences between the settling times among the control strategies in most cases.

With respect to the reactor power changes in steps and in ramps, as well as with respect to the load rejections, the computer simulation and the PLS test results have indicated similar relative performance trends for the control strategies. The IMPC method has consistently shown improved capability for set point tracking in all these simulation and tests, although the improvements on the PLS are marginal. Furthermore, both the SMPC and the IMPC have shown similar capabilities for rejecting the effect of flow disturbances in the computer simulation, as well as in the PLS tests.

Based on all these observations, it can be concluded that the IMPC has a strong potential to become a feasible methodology for the SGL control in NPPs to cover all operating conditions over all power levels.

### 6.3 **Future work**

The PLS simulation has provided some insights on the performance of the MPC based control strategies with real systems. However, it is not a real SG. More research needs to be done in order to evaluate the performance of the SMPC and the IMPC in a more realistic set up of a SG in a NPP.

Furthermore, the IMPC scheme that has been evaluated in this study is based on certain values for the elements of the weight matrix  $Q_{\text{IMPC}}$ . These values have been computed by using a simple heuristic method. Clearly, the  $Q_{\text{IMPC}}$  matrix selected in this study are not optimal. Therefore, more research needs to be done to develop effective algorithms and methodology that can compute optimal values for these elements for all power levels.

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### **Research interest**

Design and upgrade of control systems, and optimal controller tuning.

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1989 – 1999: Taught industrial control, control systems and electronics as a part time instructor at the Tabriz University in Iran.

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#### **Publication s**

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