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6-2021

## Simplified structural analysis of framed ordinary non-tempered glass panels during fire exposure

Amer Sabsabi

*The University of Western Ontario*

Maged A. Youssef

*Western University, youssef@uwo.ca*

Salah El-Din F. El-Fitiary

*The University of Western Ontario*

Ajitanshu Vedrtam

*Invertis University*

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### Citation of this paper:

Sabsabi A., Youssef M.A., El-Fitiary SF, Vedrtam A, 2021, "Simplified structural analysis of framed ordinary non-tempered glass panels during fire exposure", *Fire Safety Journal*, 122: 103357, <https://doi.org/10.1016/j.firesaf.2021.103357>

# 1 **Simplified Structural Analysis of Framed Ordinary Non-Tempered Glass Panels** 2 **during Fire Exposure**

3 A. Sabsabi <sup>1</sup>, M.A. Youssef <sup>1,\*</sup>, S.F. El-Fitiary <sup>1,2</sup>, A. Vedrtnam <sup>3</sup>

4 <sup>1</sup> *Western University, Department of Civil and Environmental Engineering, London, ON, N6A 5B9 Canada.*

5 <sup>2</sup> *Alexandria University, Department of Structural Engineering, Alexandria, Egypt*

6 <sup>3</sup> *Invertis University, Department of Mechanical Engineering, Bareilly, UP, India-243001*

## 7 **Abstract**

8 Ordinary non-tempered glass is one of the most widely used materials in the construction  
9 industry. Knowing its fire resistance is essential to ensure the safety of emergency personnel  
10 as its failure increases the oxygen supply and causes a rapid spread of the fire (flashover  
11 phenomenon). Existing approaches for evaluating the structural fire safety of glass façades  
12 require expensive experimental tests and/or extensive knowledge of Finite Element modeling.  
13 This paper provides a simplified, rational, and reliable approach to assess the structural capacity  
14 of ordinary glass panels during fire exposure. A simplified method is developed to predict the  
15 temperature difference between the edge and the center of the glass panel. Afterwards, a  
16 method, based on strain-equilibrium, is developed to predict the corresponding maximum  
17 thermal stress. The developed methods are validated by comparisons with experimental work  
18 by others.

19 **Keywords:** Façade; glass; fire exposure; thermal exposure; Finite Element, numerical  
20 modelling

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23 \* Corresponding Author. Tel.: +1 519 661 2111, 88661; E-mail address: [youssef@uwo.ca](mailto:youssef@uwo.ca)  
24 (Youssef, M.A.).  
25

## 1 **1. Introduction**

2 Fire safety has been mostly restricted to structural elements. Consequently, the interaction  
3 between the non-structural elements, e.g. glazing and façade elements, and the fire has been  
4 overlooked [1]. Nevertheless, recent tragic incidents (e.g., Grenfell Tower fire, UK)  
5 emphasized the key role of non-structural elements during fire incidents [2].

6 During a fire incident, failure of glass panels creates new vents, which increases the oxygen  
7 supply, leading to a wide spread of smoke and flames. This failure is caused by the thermal  
8 gradient between the center and edge of the glass panels [3–5]. These thermal gradients occur  
9 because of the thermal isolation provided by the supporting frame and the glass low thermal  
10 conductivity. Ordinary glass or float glass is the basic product of the floating process and is  
11 mainly composed of silica with other added oxides to improve its chemical and physical  
12 properties. It is usually non-tempered, which mean it has minimal residual stresses at its  
13 surface.

14 Several experimental [6–15] and numerical studies [16–19] were conducted to predict the  
15 thermal and structural behavior of glass panels during fire incidents. These studies highlighted  
16 the key factors, which affect the fire resistance of glass panels, including the applied heat flux  
17 [7,20], fire location [8,9], temperature gradients [14], size of glass panels [12,18,19], edge  
18 finishing conditions [16], and installation method [13,21]. The finite element models [16–19]  
19 relied on the experimentally measured temperatures to define the boundary conditions. To  
20 estimate the glass temperature numerically, Pagni and Joshi [4] proposed a dimensionless  
21 equation that can be used to predict the temperature field in glass panels during fire exposure.  
22 However, the equation is mathematically complex to solve as it requires computing three  
23 kernels and a complementary error function. Harada et al. [7] proposed an equation to calculate  
24 the thermal breakage stress for glass panels during fire exposure as a function of the

1 temperature difference between the center and edge of the glass panel. However, the breakage  
2 stress was assumed to be independent of the glass panel dimensions.

3 Much of the current literature about fire safety of glass relies on experiments or advanced  
4 analysis using finite element method. These approaches are expensive and/or time-consuming.  
5 To the best of the authors' knowledge, the literature is lacking simplified analysis techniques  
6 that can facilitate applying performance-based design concepts, while designing building  
7 facades. This paper addresses this research gap by providing a simple approach to accurately  
8 predict the thermal stresses in framed ordinary non-tempered glass panels during fire exposure.  
9 The approach provides the means to predict the temperature gradient caused by fire exposure  
10 and then, predict the maximum developed thermal stress.

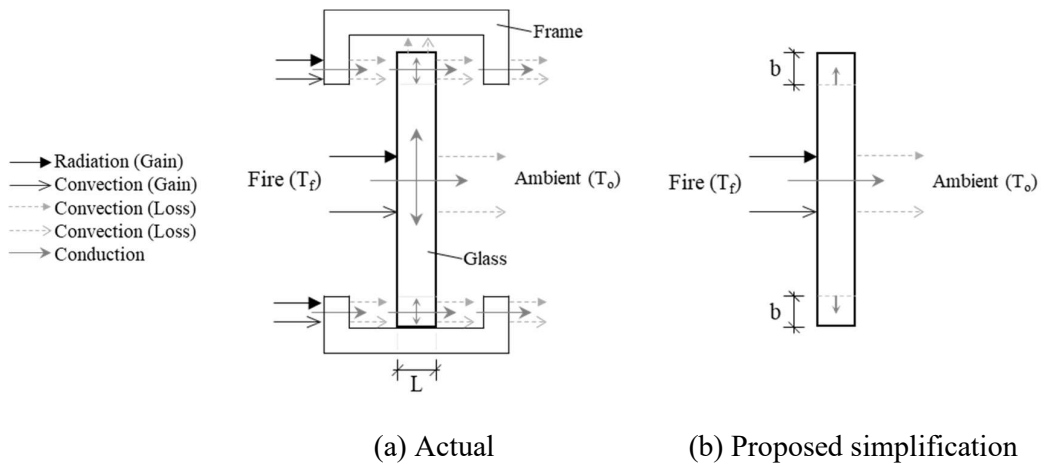
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## 12 **2. Temperature of Glass during Fire Exposure**

13 In this section, a simplified approach is developed to predict the temperatures at the center  
14 and at the edge of glass panels exposed to fire. The part of the glass panel, which is covered by  
15 the supporting frame, is assumed to be unaffected by radiation and convection of the flames.  
16 Therefore, it is only heated through conduction from the exposed part of the glass. This  
17 assumption simplifies the complex heat transfer system, shown in Fig. 1a, and eliminates the  
18 need for considering the heat exchange between the frame and glass leading to a simple heat  
19 transfer system, which is shown in Fig. 1b. This assumption will result in a higher estimate for  
20 the temperature difference in the glass panel, which will lead to a conservative estimate for its  
21 fire endurance. The approach starts by deriving a heat transfer equation to determine the  
22 temperature at the center of the glass panel, and then, uses this temperature to evaluate the  
23 temperature of the protected part.

24

1



**Fig. 1.** Heat transfer system for glass during fire exposure

## 2 2.1 Temperature at the center of the glass panel

3 During an actual fire, temperature of the glass panel depends on many factors including the  
4 location of the fire relative to the panel, size of the panel, and air movement within the  
5 compartment. In this paper, it is assumed that the uncovered glass surface is exposed to a  
6 uniform fire temperature. This assumption has been previously used in the literature [18–24].  
7 Furthermore, the temperature gradient across the glass panel thickness is assumed to be  
8 uniform. This assumption is based on the fact that the Biot number ( $Bi = \frac{hL_c}{\lambda}$ ) of typical glass  
9 panels is expected to be less than or equal 0.1, where  $L_c$  can be taken equal to the glass thickness  
10 ( $L$ ). such a value for  $Bi$  means that the resistance to conduction within the glass is much less  
11 than the resistance to convection at the air boundary layer [25].

12 Given the above-mentioned assumptions and knowing that energy generated within the  
13 glass is zero, the conservation of energy at any time instant  $t$  for the system shown in Fig. 1b  
14 can be expressed by Eq. 1,

$$\dot{E}_{in} - \dot{E}_{out} = \frac{dE_{st}}{dt} \quad (1)$$

1 Where  $\dot{E}_{in}$  and  $\dot{E}_{out}$  are the rates of energy transferred into and out of the glass panel,  
 2 respectively, and  $E_{st}$  is the rate of energy stored in the system. As the energy transfer is  
 3 happening due to convection and radiation, Eq. 1 can be rewritten in the following form,

$$q_{gain,con} + q_{gain,rad} - q_{loss,con} - q_{loss,rad} = \rho c \frac{dT}{dt} \quad (2)$$

4 Where  $q_{gain,con}$  and  $q_{gain,rad}$  are the rates of heat gain from convection and radiation,  
 5 respectively, and  $q_{loss,con}$  and  $q_{loss,rad}$  are the rates of heat loss from convection and radiation,  
 6 respectively.  $\rho$  and  $c$  are the glass' density and specific heat, respectively. Substituting with  
 7 the convection and radiation heat rate equations, Eq. 2 can be written as,

$$\Delta T = \frac{\Delta t}{\rho c L} [h_f(T_\infty - T_g) + \varepsilon \sigma (T_\infty^4 - T_g^4) - h_b(T_g - T_i) - \varepsilon \sigma (T_g^4 - T_i^4)] \quad (3)$$

8 Where  $\Delta t$  is the time increment,  $\varepsilon$  is the emissivity of the glass and can be assumed equal to  
 9 0.85 [22],  $\sigma$  is the Stefan–Boltzmann constant, and  $h_f$  and  $h_b$  are the film coefficients at the  
 10 fire and ambient sides, respectively. Eq. 3 can be utilized to calculate the temperature of the  
 11 glass at each time step for both standard and natural fire curves using a simplified spreadsheet.

12 The values of  $h_f$  and  $h_b$  can be computed utilizing existing empirical equations by  
 13 Incropera et al. [25]. For the case of vertical glass panel, the value of  $h$  can be calculated using  
 14 the following empirical equation,

$$h = \frac{0.59 \cdot k \cdot (G_r P_r)^{\frac{1}{4}}}{l} \quad (4)$$

15 Where,  $l$  is the flame height and can be taken equal to the window height,  $k$  is the thermal  
 16 conductivity of air,  $G_r$  is Grashof number,  $P_r$  is Prandtl number, and  $G_r$  and  $P_r$  can be computed  
 17 from the following equations,

$$G_r = \frac{g \cdot l^3 \cdot \beta \cdot (T_\infty - T_g)}{\nu_a^2} \quad (5)$$

$$P_r = \frac{\nu_a}{\alpha} \quad (6)$$

$$\beta = \frac{1}{T_f} \quad (7)$$

1 Where,  $T_\infty$  is the temperature of the air,  $T_g$  is the temperature of the glass surface,  $g$  is the  
 2 gravitational acceleration,  $\nu_a$  is the kinematic viscosity of the air,  $\alpha$  is the thermal diffusivity  
 3 of the air,  $\beta$  is the thermal expansion coefficient of the air, and  $T_f$  is the film temperature and  
 4 can be calculated as the average temperature between the air and the glass surface [26]. The air  
 5 temperature is taken equal to the fire temperature at the exposed side of the glass and the  
 6 ambient temperature ( $T_i$ ) at the unexposed side of the glass. Eq. 4 can be used based on a  
 7 conservative and widely used assumption in structural fire engineering, which assumes the fire  
 8 and air are stagnant inside the fire compartment. This assumption leads to free convection  
 9 between the air and the glass panel. For this case, the convection heat transfer coefficient, film  
 10 coefficient ( $h$ ), typically ranges from 5 to 25 W/m<sup>2</sup>K [27].

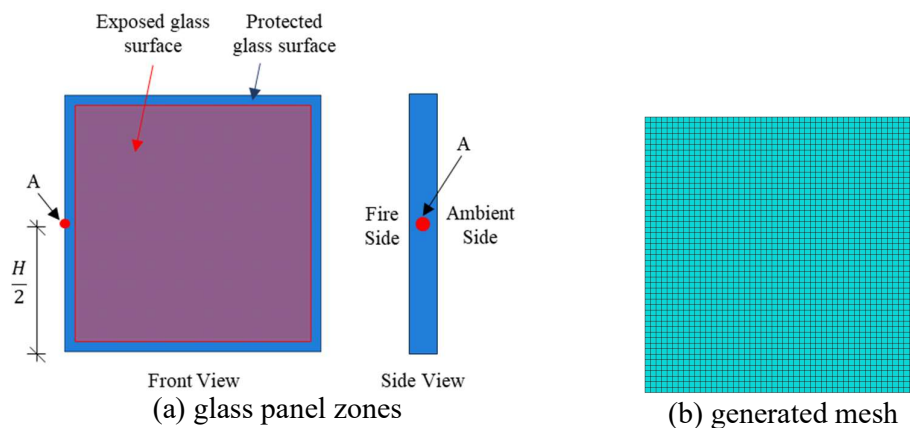
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## 12 **2.2 Temperature at the edge of the glass panel**

13 Based on the assumption that the edge of the glass panel is only heated via conduction from  
 14 the exposed parts, a parametric study was necessary to determine the ratio between the  
 15 temperature of the protected part ( $T_e$ ) and the temperature of the exposed part ( $T_g$ ). The  
 16 commercial software ABAQUS [28] was utilized for that purpose. Heating of the exposed part  
 17 of the glass, Fig. 2a, was simulated as uniform surface interaction that involved radiation and  
 18 convection. For such a case, the change in the glass dimensions do not affect the ratio between  
 19  $T_e$  and  $T_g$ . The only parameters that need to be considered are the glass thickness (L), width of  
 20 the frame (b), and the fire scenario. Fifteen Glass thicknesses covering range from 1 to 15 mm

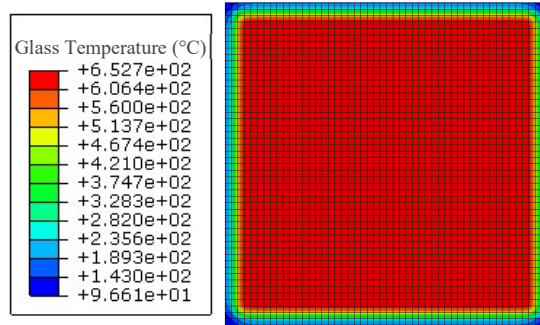
1 and ten widths for the supporting frame covering range from 5 to 50 mm were considered in  
2 the analysis. These ranges deemed to cover most of the practical values available in the  
3 literature. Assuming ISO 834 temperature-time relationship [29], 150 cases were analyzed. It  
4 should be noted that the analysis cases also represent the heating region of natural fire curves.

5 The material properties were assumed as follows  $\rho = 2500 \text{ kg/m}^3$  and  $c = 820 \text{ J/kg}\cdot\text{K}$ . The  
6 glass was initially assumed to be at the ambient temperature,  $T_i$  of  $20^\circ\text{C}$ , and heat losses were  
7 assumed to only occur at the ambient side. The glass panel was modeled using 8-node-3D  
8 linear-heat transfer brick elements (DC3D8 type from ABAQUS library). A maximum mesh  
9 size of 10 mm was utilized, as it was found to result in acceptable accuracy. Using a smaller  
10 mesh size did not affect the accuracy of the results, and significantly increased the  
11 computational time. For example, reducing the mesh size from 10 mm to 5 mm did not change  
12 the value of  $T_g$  and resulted in  $T_e$  difference of less than 5%, but it increased the computation  
13 time by 180%. An example of the generated mesh is shown in Fig. 2b. The average temperature  
14 at point A, which is at the middle of the glass panel edge, as shown in Fig. 2a, was recorded  
15 for each run. A typical temperature distribution, as produced by ABAQUS, is shown in Fig. 3.  
16 Also, the typical variation of the ratio  $\frac{T_e}{T_g}$  with time is shown in Fig. 4.

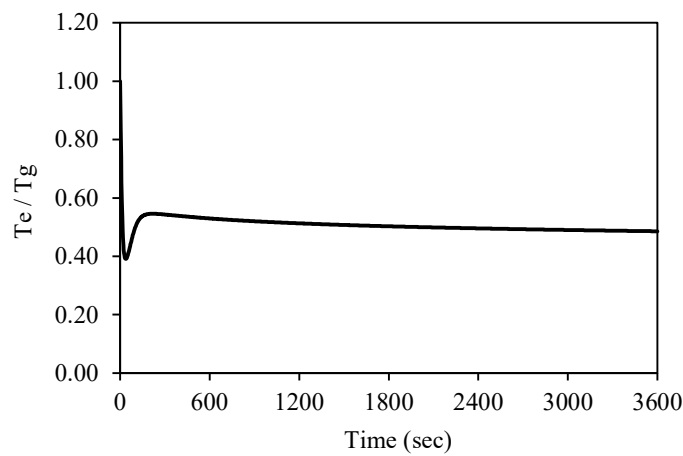


**Fig. 2.** Glass Panel Simulation using ABAQUS





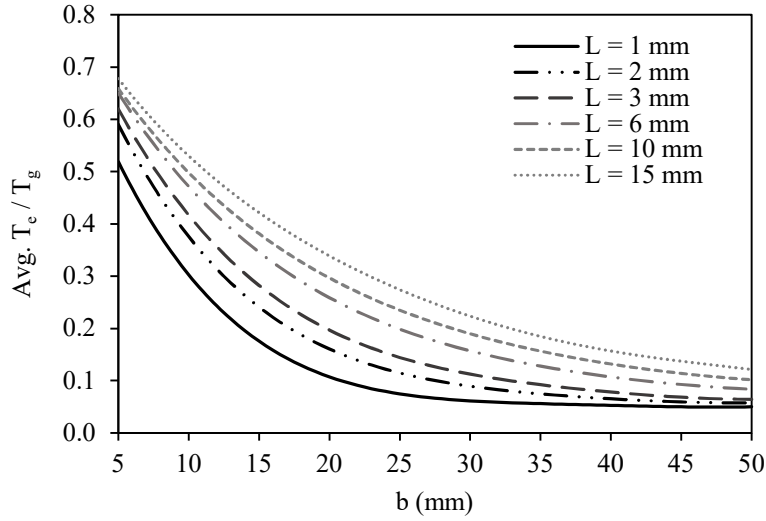
**Fig. 3.** ABAQUS Temperature Distribution (L = 6 mm, b = 20 mm, t = 30 minutes)



**Fig. 4.** Variation of  $\frac{T_e}{T_g}$  with time (L = 1 mm and b = 5 mm)

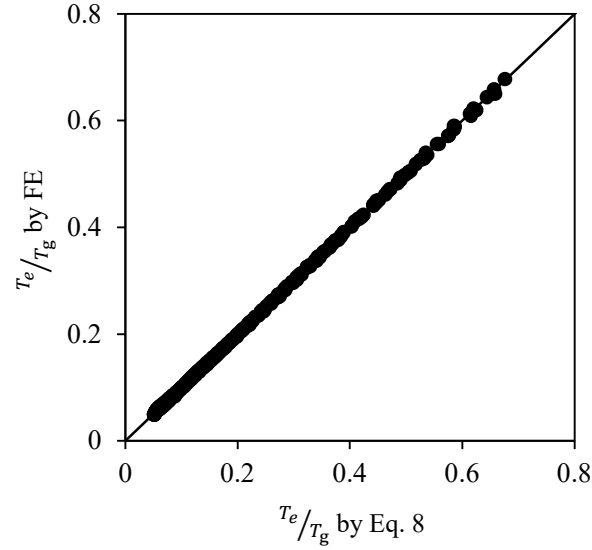
1 Initially, the exposed and protected parts of the glass had the same temperature, and, then the  
 2 ratio between their temperatures started to change until reaching a constant value. Considering  
 3 all examined cases, the average  $\frac{T_e}{T_g}$ , for the relatively constant part of the variation, is given in  
 4 Fig. 5 as function of the frame width and glass thickness. The temperature difference between  
 5 the center and edge of the glass panel increases with increasing the glass thickness and  
 6 decreases with increasing the frame width. Engineers can utilize this figure to calculate this  
 7 ratio, which can be used calculate the temperature of the glass edge in terms of the temperature  
 8 at the glass center. To further simplify calculation of  $\frac{T_e}{T_g}$ , the figure data were utilized to develop

1 the formula given by Eq. 8, which allow calculating  $\frac{T_e}{T_g}$  as function of  $b$  (m) and  $L$  (m). The  
 2 equation and coefficients were determined using a least square regression analysis, common  
 3 regression requirements of probability ( $p$ ) < 0.0001 and correlation ( $R^2_{adj}$ ) > 95% were  
 4 maintained. The maximum error associated with using Eq. 8 is less than 6%, as shown in Fig.  
 5 6.



**Fig. 5.** Evaluation of  $\frac{T_e}{T_g}$  as function of  $b$  and  $L$

$$\begin{aligned}
 \frac{T_e}{T_g} = & + 0.739 \times 10^0 \times 1 & - 81.44 \times 10^0 \times b & (8) \\
 & + 134.7 \times 10^0 \times L & + 833.5 \times 10^0 \times b \times L & \\
 & + 3.345 \times 10^3 \times b^2 & - 31.25 \times 10^3 \times L^2 & \\
 & - 201.6 \times 10^3 \times b^2 \times L & + 606.4 \times 10^3 \times b \times L^2 & \\
 & - 62.69 \times 10^3 \times b^3 & + 3.160 \times 10^6 \times L^3 & \\
 & + 2.300 \times 10^6 \times b^2 \times L^2 & + 3.550 \times 10^6 \times b^3 \times L & \\
 & - 52.00 \times 10^6 \times b \times L^3 & + 536.0 \times 10^3 \times b^4 & \\
 & - 155.0 \times 10^6 \times L^4 & - 55.40 \times 10^6 \times b^3 \times L^2 & \\
 & + 101.0 \times 10^6 \times b^2 \times L^3 & - 17.60 \times 10^6 \times b^4 \times L & \\
 & + 1.280 \times 10^9 \times b \times L^4 & - 1.590 \times 10^6 \times b^5 & \\
 & + 3.040 \times 10^9 \times L^5 & &
 \end{aligned}$$



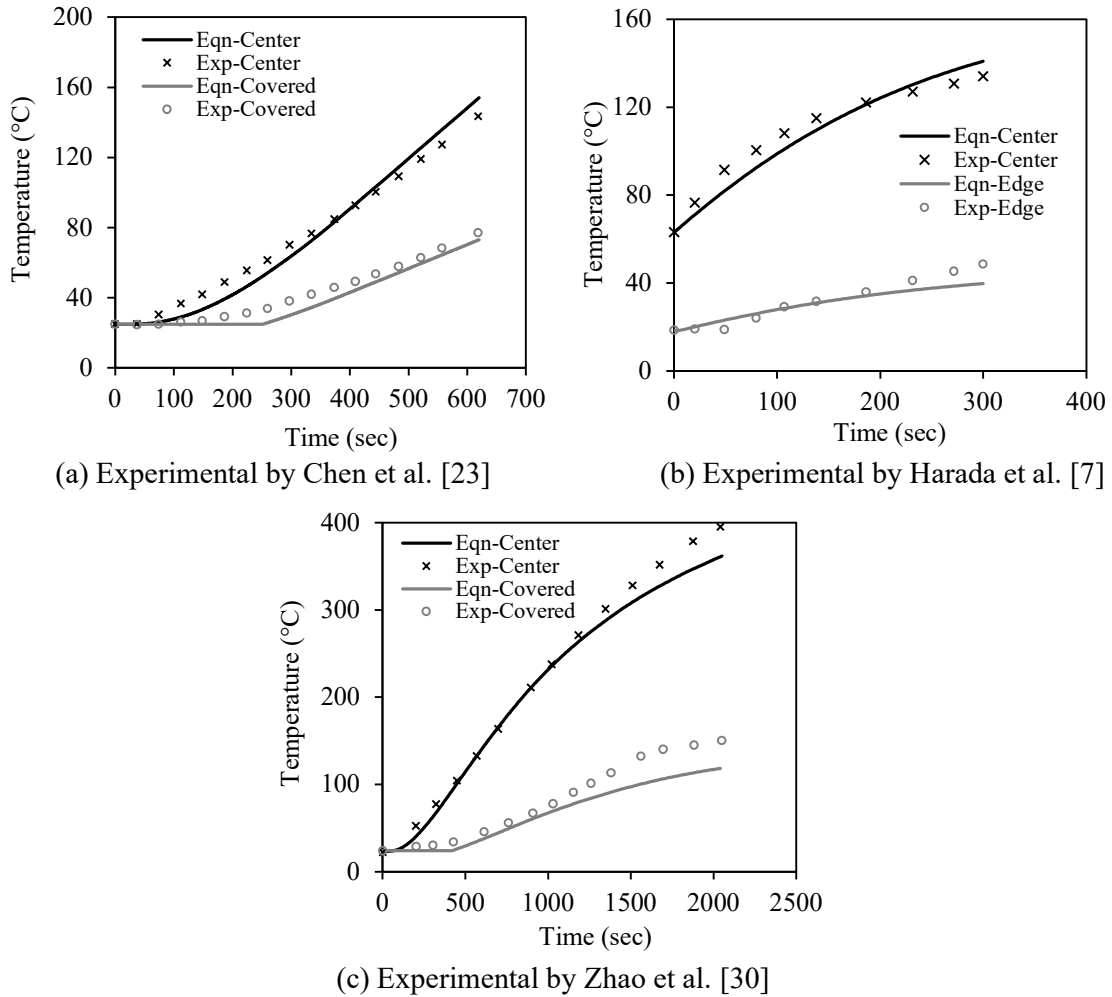
**Fig. 6.** Accuracy of using Eq. 8 in predicting  $\frac{T_e}{T_g}$

### 1 2.3 Validation

2 The experimental test conducted by Chen et al. [23] was utilized to validate the proposed  
 3 heat transfer method. Test 1 by Chen et al. [25] involved heating a 600 mm by 600 mm by 6  
 4 mm ordinary glass panel using a natural fire curve. The width of the protected part was 10 mm.  
 5 Eq. 3 was first used to predict the temperature at the glass center. Afterward,  $\frac{T_e}{T_g}$  was evaluated  
 6 using Eq. 8 and found to be equal to 0.474. As shown in Fig. 7a, the results of the proposed  
 7 approach are in good agreement with the experimental study. It should be noted that Eq. 8 is  
 8 only valid after the ratio  $\frac{T_e}{T_g}$  becomes constant, which is at about 250 second for this sample.  
 9 However, the use of a constant ambient temperature for the duration before the 250 second  
 10 seems to provide good results.

11 To further validate the proposed method, the experimental tests conducted by Harada et al.  
 12 [7] and Zhao et al. [30] were considered. The glass panel dimensions were 500 mm by 500 mm  
 13 by 3 mm and 600 mm by 600 mm by 6 mm, respectively. The width of the covered part was  
 14 15 mm and 10 mm, respectively. Figs. 7b and 7c show that the proposed approach predicted

1 the temperature at the center and edge of the glass panels with good accuracy. The small  
 2 differences between the experimental and numerical results can be due to experimental errors,  
 3 or numerical assumptions including: (1) uniform temperature across the glass thickness, (2)  
 4 constant glass thermal properties, and (3) ignoring radiation and convection for the covered  
 5 part of the glass panel.



**Fig. 7.** Validation of the Proposed Approach

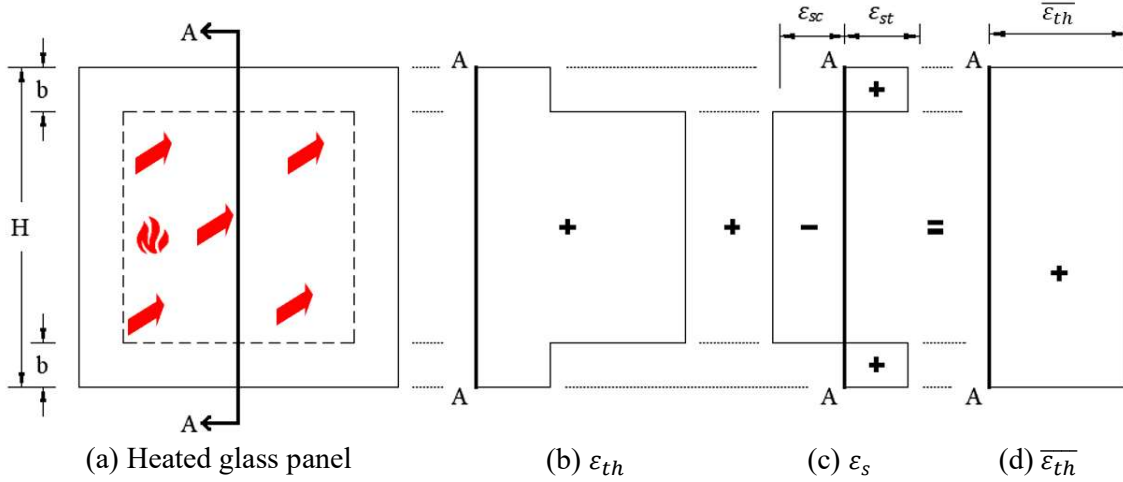
### 3. Maximum Developed Thermal Stress

The second step in the proposed approach is to determine the maximum developed thermal stress. The following subsections provide the development of a simplified method to estimate the maximum thermal stress, and then generalize the simplified method to be applicable for any temperature distribution.

#### 3.1 Proposed simplified method

Fig. 8a shows a glass panel, with dimensions  $W$  by  $H$ , and a frame width  $b$ . The connection between the panel and the frame was assumed to have enough clearance to allow for free expansion [3,10,18]. During fire exposure, the temperature in the protected part is much lower than the temperature of the exposed part. The resulting unrestrained thermal strain distribution ( $\varepsilon_{th}$ ) is shown in Fig. 8b. This free-thermal expansion cannot develop, as the glass is expected to follow the plane section assumption. Thus, a self-induced strain ( $\varepsilon_s$ ), Fig. 8c, is expected to develop to convert the free thermal strain to an equivalent linear strain ( $\overline{\varepsilon_{th}}$ ), which is uniform for the presented case because of the symmetry of the unrestrained thermal strains. The uniform strain,  $\varepsilon_i$ , shown in Fig. 8d reflects the actual deformation of the glass. This concept was previously adopted by El-Fitiany and Youssef [31], while analyzing reinforced concrete cross sections exposed to fire.

The self-induced strains must be in-self equilibrium. They can be divided into internal compressive strains ( $\varepsilon_{sc}$ ) for the exposed glass area and tensile strains ( $\varepsilon_{st}$ ) for the protected glass area (Fig. 8c). These tensile strains correspond to the maximum tensile stresses, which will develop in the glass sample.



**Fig. 8.** Developed strains in uniformly heated glass panel

1

2 Eq. 9 can be derived based on the uniform total strain, and from the equilibrium of the self-  
 3 induced forces, Eq. 10 can be written.

$$\varepsilon_{st} + \alpha_g \times T_e = \alpha_g \times T_g - \varepsilon_{sc} \quad (9)$$

$$\varepsilon_{sc} \times E \times (H - 2b) \times L = \varepsilon_{st} \times E \times 2b \times L \quad (10a)$$

$$\varepsilon_{st} = \varepsilon_{sc} \left( \frac{H}{2b} - 1 \right) \quad (10b)$$

4 Where  $\alpha_g$  and  $E$  are the glass' thermal expansion coefficient and modulus of elasticity,  
 5 respectively. The value of the self-induced tensile thermal strain can then be obtained by  
 6 solving equations 9 and 10b, which results in Eq. 11.

$$\varepsilon_{st} = \alpha_g (T_g - T_e) \left( 1 - \frac{2b}{H} \right) \quad (11)$$

7 Eq. 11 indicates that the self-induced tensile strain increases with the increase of the height of  
 8 the glass panel ( $H$ ) and the difference in temperature between the exposed and protected  
 9 regions. It decreases with the increase of width of the protected area ( $b$ ). These findings are in  
 10 agreements with the findings of previous experiments [11,18,32]. It should be noted that the

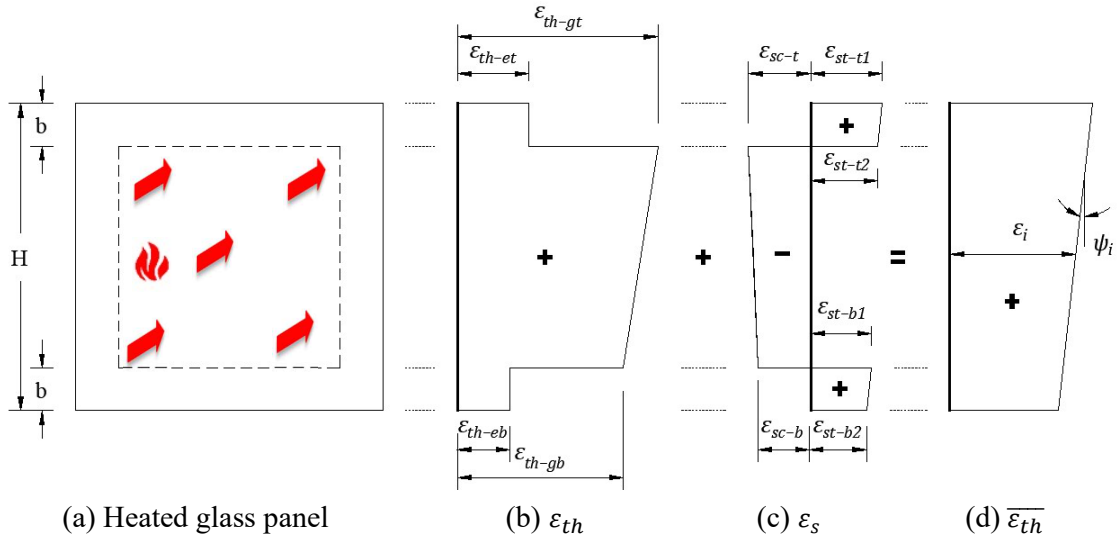
1 factor  $\left(1 - \frac{2b}{H}\right)$  is consistent with the geometric factor proposed by Pagni and Joshi [4,10] and  
2 Pagni [10], which was developed based on a hyperbolic temperature variation. Using the  
3 previously evaluated temperatures at the center and edge of the glass panel, engineers can  
4 utilize equation 11 to estimate the maximum internal thermal stress in the glass panel.

5

### 6 **3.2 Generalization of the proposed simplified method**

7 In a real fire scenario, the glass panel is expected to have a variable temperature profile.  
8 This section explores the use of the developed simplified method for the case of linearly  
9 varying temperature profile. The derivation, shown below, can be modified to accommodate  
10 other temperature distributions.

11 Fig. 9a shows a glass panel, exposed to higher average temperatures at its top than its  
12 bottom. The temperature within the width  $b$  was assumed to be constant with values  $T_{et}$  at the  
13 top and  $T_{eb}$  at the bottom. The temperature of the exposed region of the glass panel was  
14 assumed to be varying linearly from  $T_{gt}$  at the top to  $T_{gb}$  at the bottom. This linear temperature  
15 distribution is a simplification for real situations where the temperature of the upper layers of  
16 air is higher than the lower ones (stack effect) due the convection of compartment fires. The  
17 resulting unrestrained thermal strains ( $\varepsilon_{th}$ ), Fig. 9b, are  $\varepsilon_{th-et}$  at the top covered region,  $\varepsilon_{th-eb}$   
18 at the bottom covered region,  $\varepsilon_{th-gt}$  at the top of the exposed region, and  $\varepsilon_{th-gb}$  at the bottom  
19 of the exposed region. Self-induced strains ( $\varepsilon_s$ ), Fig. 9c, are expected to be developed to  
20 maintain the linearity of the thermal profile. The equivalent linear strain profile ( $\overline{\varepsilon_{th}}$ ) is  
21 expected to be variable in this case with a middle strain  $\varepsilon_i$  and a curvature  $\psi_i$ .



**Fig. 9.** Developed strains in a glass panel heated at its top more than its bottom

- 1 The self-induced thermal strains can be expressed in terms of the equivalent thermal strains
- 2 and the unrestrained thermal strains using the following equations.

$$\varepsilon_{st-t1} = \varepsilon_i + \psi_i \frac{H}{2} - \varepsilon_{th-et} \quad (12a)$$

$$\varepsilon_{st-t2} = \varepsilon_i + \psi_i \frac{H - 2b}{2} - \varepsilon_{th-et} \quad (12b)$$

$$\varepsilon_{st-b1} = \varepsilon_i - \psi_i \frac{H - 2b}{2} - \varepsilon_{th-eb} \quad (12c)$$

$$\varepsilon_{st-b2} = \varepsilon_i - \psi_i \frac{H}{2} - \varepsilon_{th-eb} \quad (12d)$$

$$\varepsilon_{sc-t} = \varepsilon_i + \psi_i \frac{H - 2b}{2} - \varepsilon_{th-gt} \quad (12e)$$

$$\varepsilon_{sc-b} = \varepsilon_i - \psi_i \frac{H - 2b}{2} - \varepsilon_{th-gb} \quad (12f)$$

- 3 Where  $\varepsilon_{st-t1}$ ,  $\varepsilon_{st-t2}$ ,  $\varepsilon_{st-b1}$  and  $\varepsilon_{st-b2}$  are the self-induced tensile strains at the top and bottom
- 4 edges of the covered areas as demonstrated in Fig. 9c.  $\varepsilon_{sc-t}$  and  $\varepsilon_{sc-b}$  are the self-induced
- 5 compressive strains at the top and bottom of the exposed part of the glass.



1 Eqs. 13 and 14 can then be derived based on equilibrium of forces and moments resulting  
2 from the self-induced strains.

$$\varepsilon_i = \frac{\alpha_g b}{H} (T_{et} + T_{eb}) + \frac{\alpha_g (H - 2b)}{2H} (T_{gt} + T_{gb}) \quad (13)$$

$$\psi_i = \frac{\alpha_g (6bH - 6b^2)}{H^3} (T_{et} - T_{eb}) + \frac{\alpha_g (H - 2b)^2}{H^3} (T_{gt} - T_{gb}) \quad (14)$$

### 3 4. Validation

4 The proposed approach is used to calculate the tensile stress generated during fire exposure  
5 of different glass panels given in the literature. Table 1 provides a summary of the validation  
6 cases. Wang et al. [18] experimentally tested ordinary non-tempered glass panels ( $E = 67$  GPa,  
7  $\rho = 2500$  kg/m<sup>3</sup>, and  $\alpha_g = 8.5 \times 10^{-6}$  1/°C) with dimensions of 300 mm by 300 mm by 6 mm,  
8 which were protected at the edges by a frame width of 20 mm. The glass panels were heated in  
9 a small air compartment using a heating panel. The heating rate was 10 °C/min until the air  
10 reached a temperature of 600 °C, which was kept constant for a period of 20 minutes. Wang et  
11 al. [18] had also developed a FE model to study the effect of the glass panel dimensions on its  
12 behavior during fire exposure. Dimensions ranging from 100 mm to 1000 mm and aspect ratios  
13 of 400:1, 100:1, 25:1, 25:4, 4:1, and 25:16 were examined. Cases 1 to 10 of the finite element  
14 analysis by Wang et al. [18] were used to validate the proposed method. Harada et al. [7]  
15 exposed ordinary non-tempered glass panels ( $E = 73$  GPa,  $\rho = 2500$  kg/m<sup>3</sup>, and  $\alpha_g = 8.75 \times$   
16  $10^{-6}$  1/°C) to heat fluxes ranging between 2.7 kW/m<sup>2</sup> and 9.7 kW/m<sup>2</sup>. The size of the glass  
17 panels was 500 mm by 500 mm by 3 mm and they were protected at the edges by a frame width  
18 of 15 mm. Wang et al. [33] developed a finite element program to investigate the thermal stress  
19 distribution during fire exposure. The program was validated using the experiments by Skelly  
20 et al. [34] on ordinary non-tempered glass panel ( $E = 70$  GPa and  $\alpha_g = 9.5 \times 10^{-6}$  1/°C) exposed

1 to pool fire. The analyzed glass panels by Wang et al. [33] had a size of 500 mm by 280 mm  
 2 by 2.4 mm and the width of the supporting frame was 25 mm. Chen et al. [11] exposed ordinary  
 3 non-tempered glass panels ( $E = 67.2 \text{ GPa}$ ,  $\rho = 2500 \text{ kg/m}^3$ , and  $\alpha_g = 8.46 \times 10^{-6} \text{ 1/}^\circ\text{C}$ ) to radiant  
 4 heating in an enclosed compartment. The glass panel size by Chen et al. [11] was 600 mm by  
 5 600 mm by 6 mm and the width of the frame was 30 mm. The measured temperature field was  
 6 implemented into a finite element program to predict the resultant stresses. Dembele et al. [16]  
 7 developed a program (Glaz3D) that was validated with ANSYS [35] to study the thermal and  
 8 mechanical behavior of glazing elements during fire. The validation results are summarized in  
 9 Fig. 10. As shown in the figure, the proposed approach predicted the fracture tensile strength  
 10 with an accuracy of  $\pm 10\%$ .

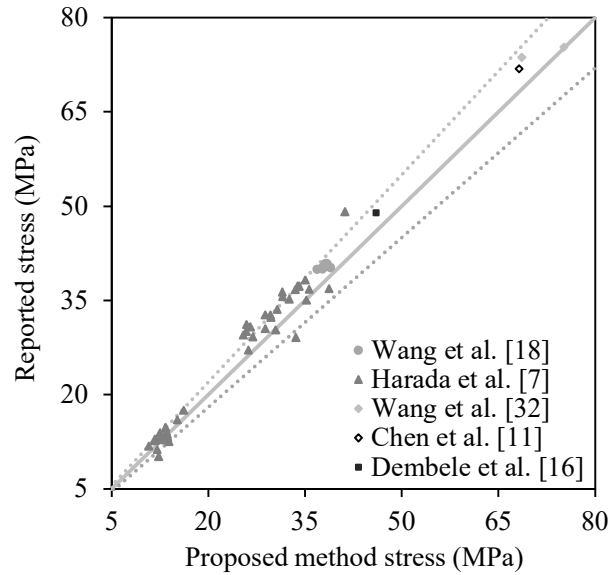
11

12

**Table 1.** Validation Cases

Parameter	Wang et al. [18]	Harada et al. [7]	Wang et al. [33]	Chen et al. [11]	Dembele et al. [16]
$E$ , ( $10^{10} \text{ Pa}$ )	6.7	7.3	7.0	6.72	7.3
$\alpha_g$ , ( $10^{-6} \text{ K}^{-1}$ )	8.5	8.75	8.5	8.46	8.75
Glass panel size, ( $\text{m}^2$ )	0.1 to 1 $\times$ 0.1 to 1	0.5 $\times$ 0.5	0.50 $\times$ 0.28	0.6 $\times$ 0.6	0.3 $\times$ 0.3
Thickness, L (m)	0.006	0.003	0.0024	0.006	0.003
Covered part, b, (m)	0.02	0.015	0.025	0.03	0.015
Max. temperature difference ( $^\circ\text{C}$ )	67 – 150	17 – 70	143	133	80

13



**Fig. 10.** Validation results

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2

3

#### 4 **5. Conclusions**

5 This paper provides a simple yet reliable approach to assess the behavior of ordinary glass  
 6 panels during fire exposure. A set of simplified methods were developed to conduct both heat  
 7 transfer and stress calculations.

8 For heat transfer calculations, a simplified method to estimate the temperature at the center  
 9 of the glass panel was proposed. The method assumes that the temperature across the glass  
 10 thickness is constant. The finite element method was then utilized to develop an equation that  
 11 relates the temperature at the edge of the panel to the temperature at its center. The proposed  
 12 equation suggests that the temperature difference between the glass center and edge increases  
 13 with the increase of glass thickness and decreases with the increase of the frame width. For  
 14 stress calculations, a simplified method to estimate the self-induced thermal strains, which  
 15 maintain the plane section assumption, is developed considering cases of uniform fire exposure  
 16 and non-uniform fire exposure. Predictions of the proposed approach were compared to the  
 17 experimental and numerical work by others. The results from the proposed approach confirm

1 the findings of previous experiments that the self-induced tensile stress increases with the  
2 increase of the glass panel dimensions and decreases with the increase of the frame width.

3 The proposed approach can be utilized to estimate the maximum temperature difference  
4 within a glass panel and calculate the developed thermal stresses in glass panels during fire  
5 exposure. Future research is needed to extend the applicability of the proposed approach to: (1)  
6 other glass types, (2) other conditions of fire exposure, where the resulting temperature of the  
7 exposed part of the glass panel is not uniform (partially exposed panel), (3) cases where the  
8 heat exchange between the glass and the frame need to be considered, (4) cases with moving  
9 air and fire, and (5) glass panels with large dimensions. Notwithstanding these limitations, the  
10 comparisons with existing experimental work have confirmed the accuracy of the proposed  
11 approach in estimating the maximum tensile stress developed during fire exposure, and thus its  
12 accuracy to predict the breakage of ordinary glass, which almost coincides with its cracking  
13 [3,7,11,34].

14

### 15 **Acknowledgments**

16 The present study was financially supported by the India-Canada Center for Innovative  
17 Multidisciplinary Partnerships to Accelerate Community Transformation and Sustainability  
18 (IC-IMPACTS), Canada.

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